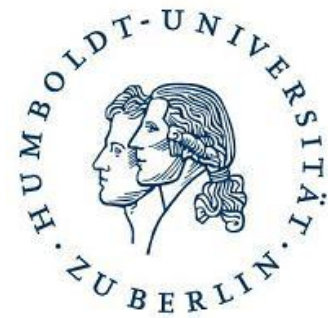


SUMMERSOC

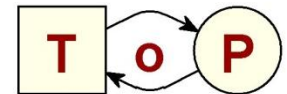
Hersonissos, Wednesday, June 27, 2018. 9.30 – 10.30



Conceptual Fundamentals of Reactive Systems



*Same place as
Christoph Freytag*



Theory of
Programming

Prof. Dr. W. Reisig

Wolfgang Reisig

Humboldt-Universität zu Berlin

Conceptual Fundamentals of Reactive Systems

What could this be?

*Identify the (??) fundamental concepts
and build a theory on top of this ...*

We are so wonderfully progressing without
... for a while

There is this deep “Theoretical Informatics” stuff. That’s enough.
No. There is something fundamentally new

What to do with such a conceptual fundament?
*to make it conceptually simpler,
better teachable,
better usable, also by non-experts*

e.g. PAXOS

Road map

1. Components and composition:
the basic paradigm for communication
2. Fundamental properties of the composition operator
3. Components' contents
4. ... even more general

Road map

- 1. Components and composition:
the basic paradigm for communication**
2. Fundamental properties of the composition operator
3. Components' contents
4. ... even more general

An analogy: Classical computing

Turing machine:

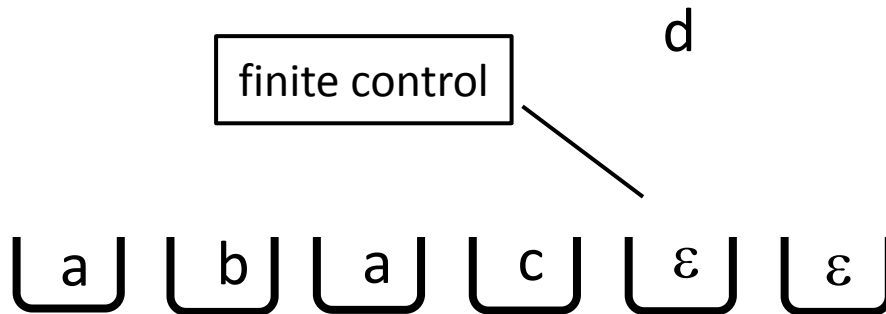
A sequence of containers

Each container

holds a symbol

actual container

can be updated



The starting point for
computable functions

The starting point for react. systems ...?

Reactive systems are *fundamentally* different.

Don't compute functions at all

Are not intended to terminate

Can not be abstracted to *one* device

...

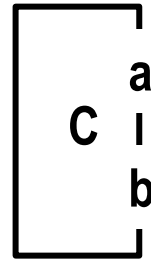
... requires a fundamentally new computation model

A *system* consists of *components*.

Each component has an *interface*.

An interface contains *gates*.

Components are *composed*
by gluing *matching gates*



Literature describes many such system models

A system consists of *components*.

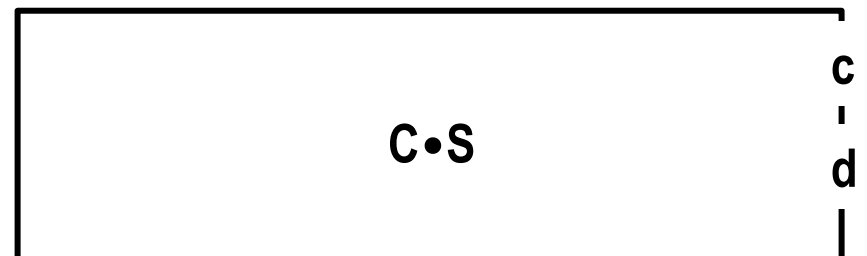
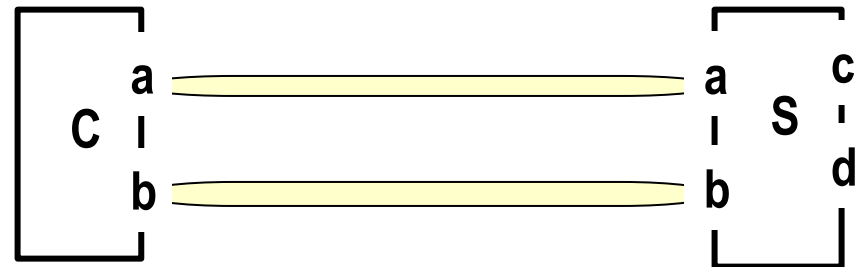
Each gate has a *label*.

Equally labeled gates *match*.

Each component has an *interface*.

An interface contains *gates*.

Components are *composed* by gluing *matching gates*



A small, but decisive variant

A system consists of *components*.

Each component ~~has an interface~~.

A has *two* interfaces, ***A** and **A***.

An interface contains *gates*.

Components **A** and **B** are *composed*

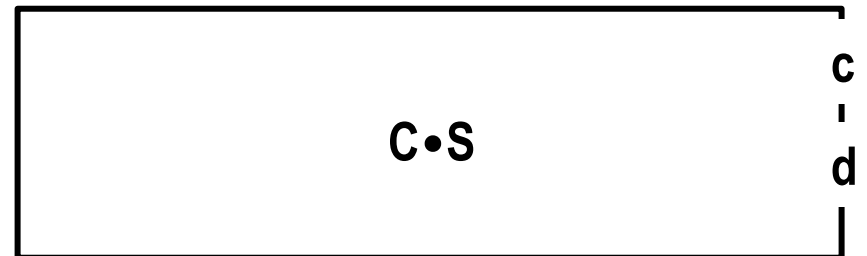
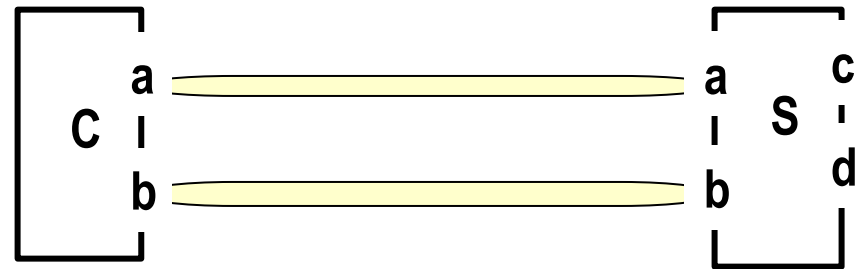
by gluing *matching gates*

of **A*** and ***B**.

Each gate has a *label*.

Equally labeled gates

of **A*** and ***B** match.



A small, but decisive variant

A system consists of *components*.

Each component ~~has an interface~~.

A has *two* interfaces, ***A** and **A***.

An interface contains *gates*.

Components **A** and **B** are *composed*

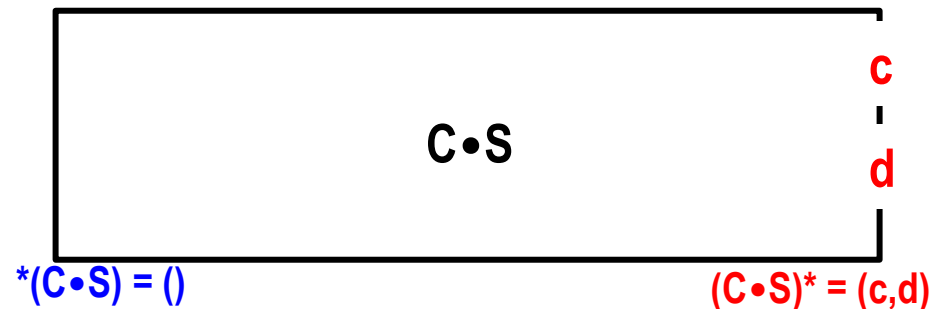
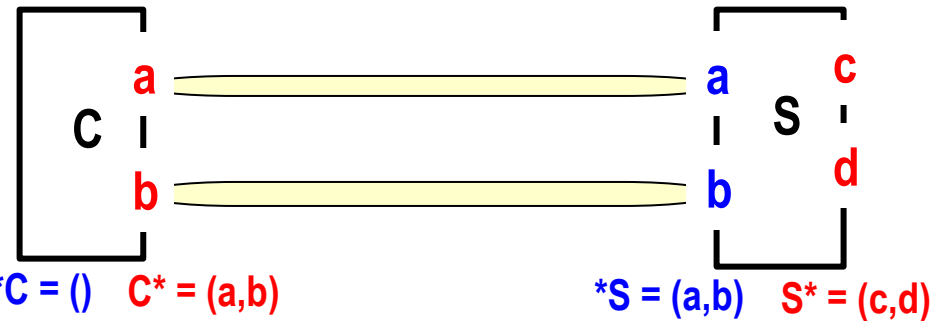
by gluing *matching gates*

of **A*** and ***B**.

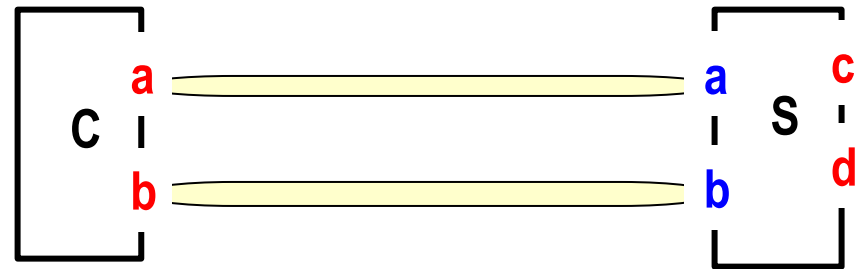
Each gate has a *label*.

Equally labeled gates

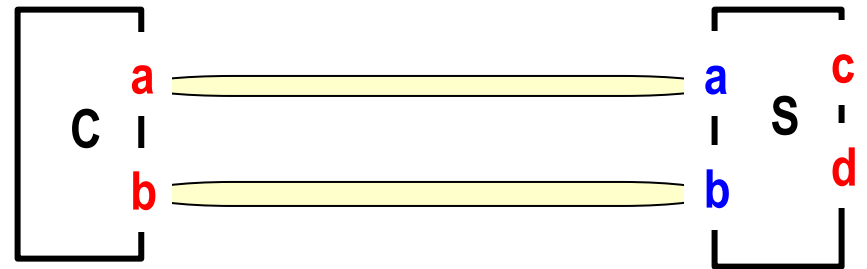
of **A*** and ***B** match.

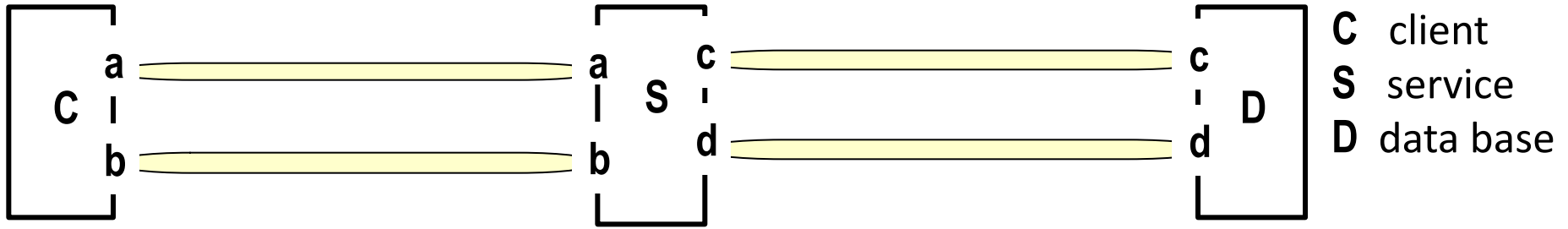


A small exercise: operating system architecture



A small exercise: operating system architecture

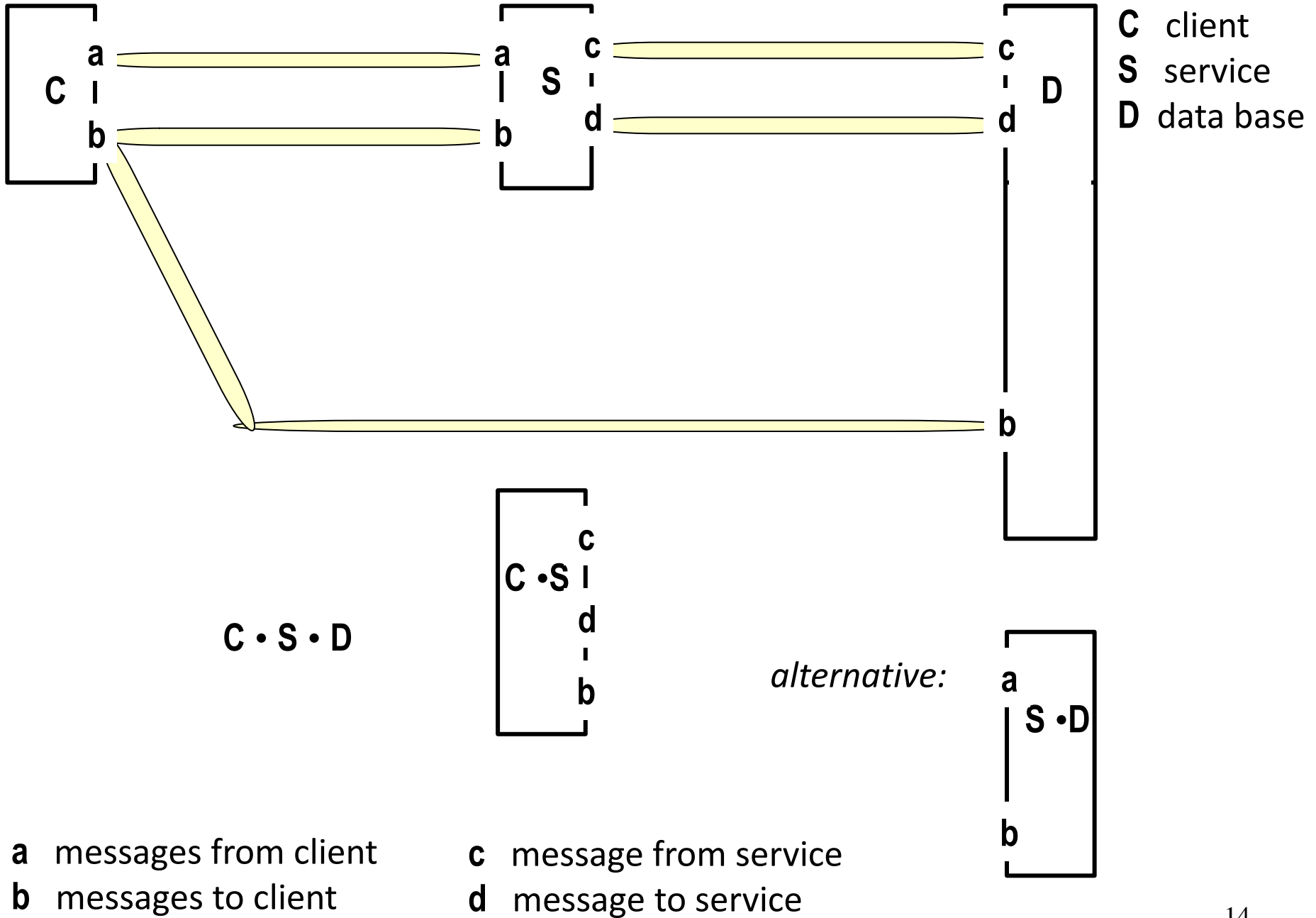


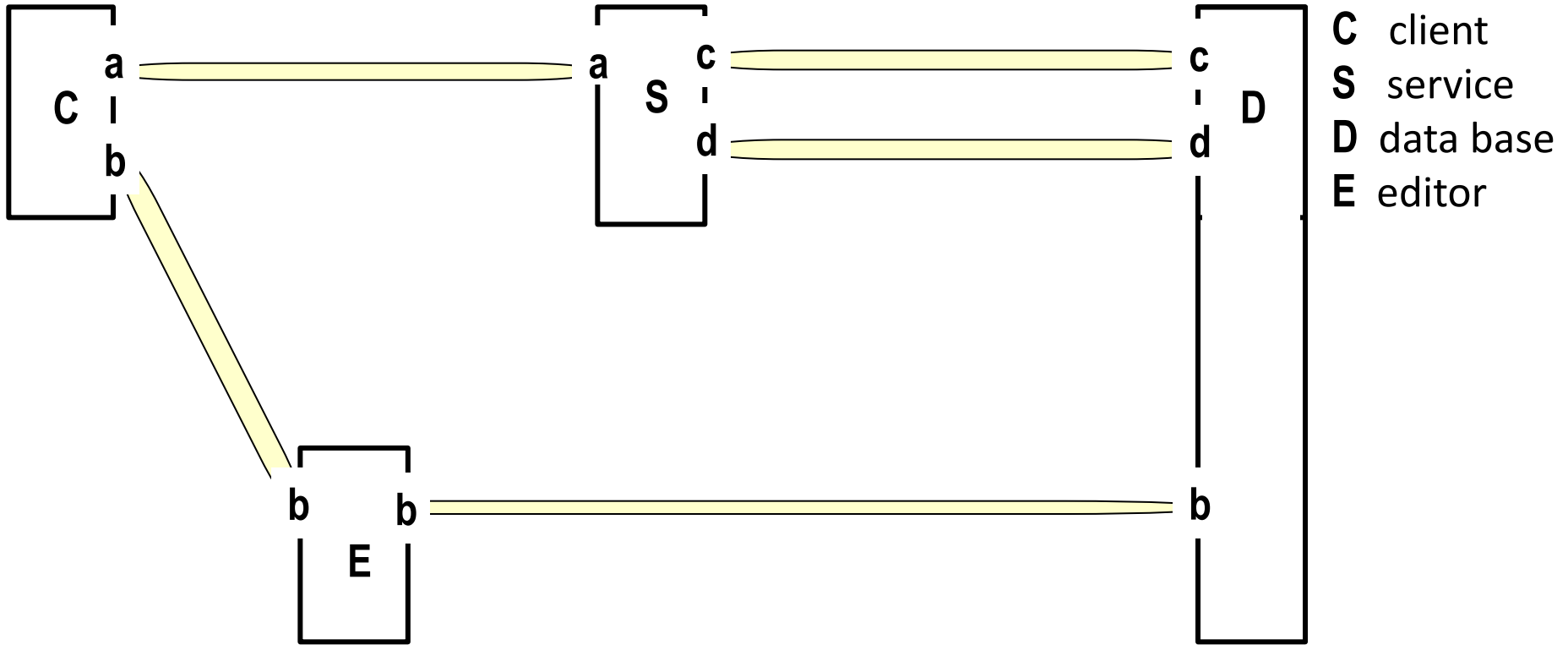


C • S • D

a messages from client
b messages to client

c message from service
d message to service





C • E • S • D

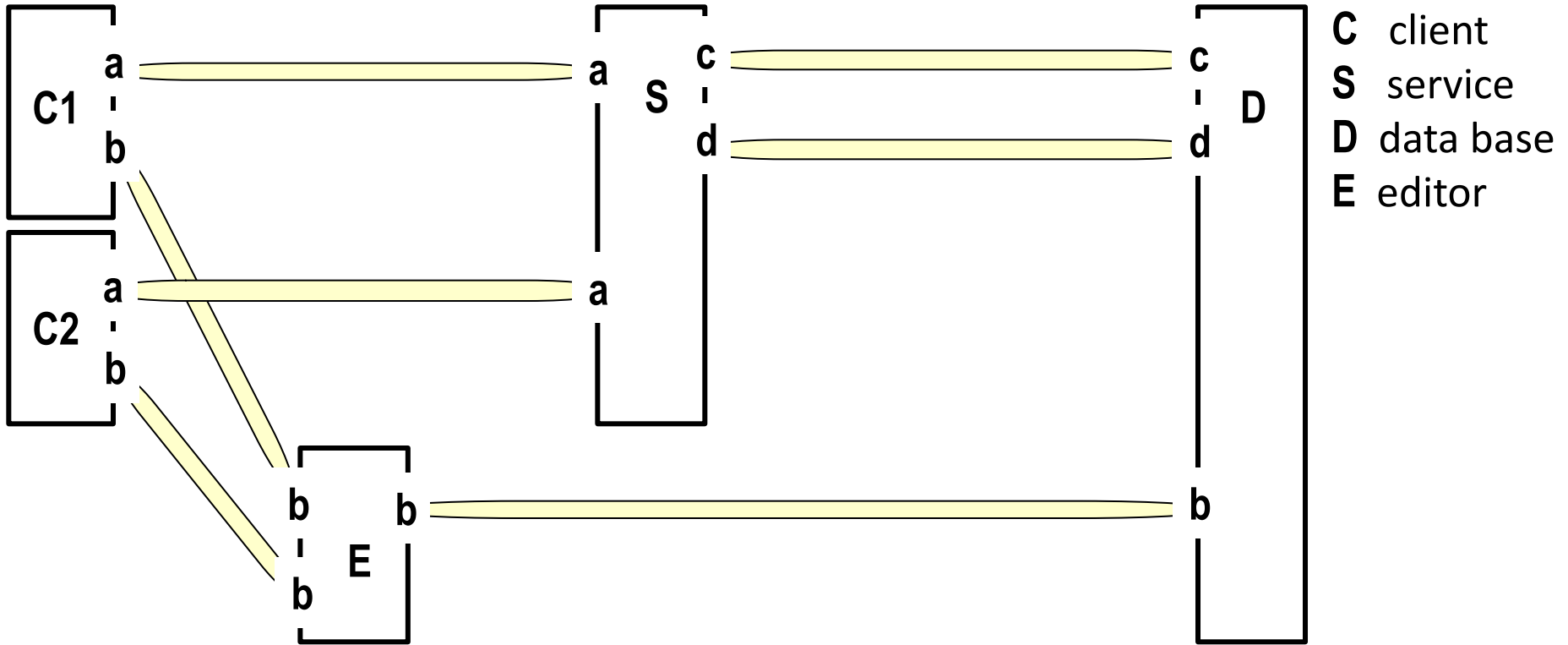
C • S • E • D

a messages from client

b messages to client

c message from service

d message to service



C1 • C2 • E • S • D

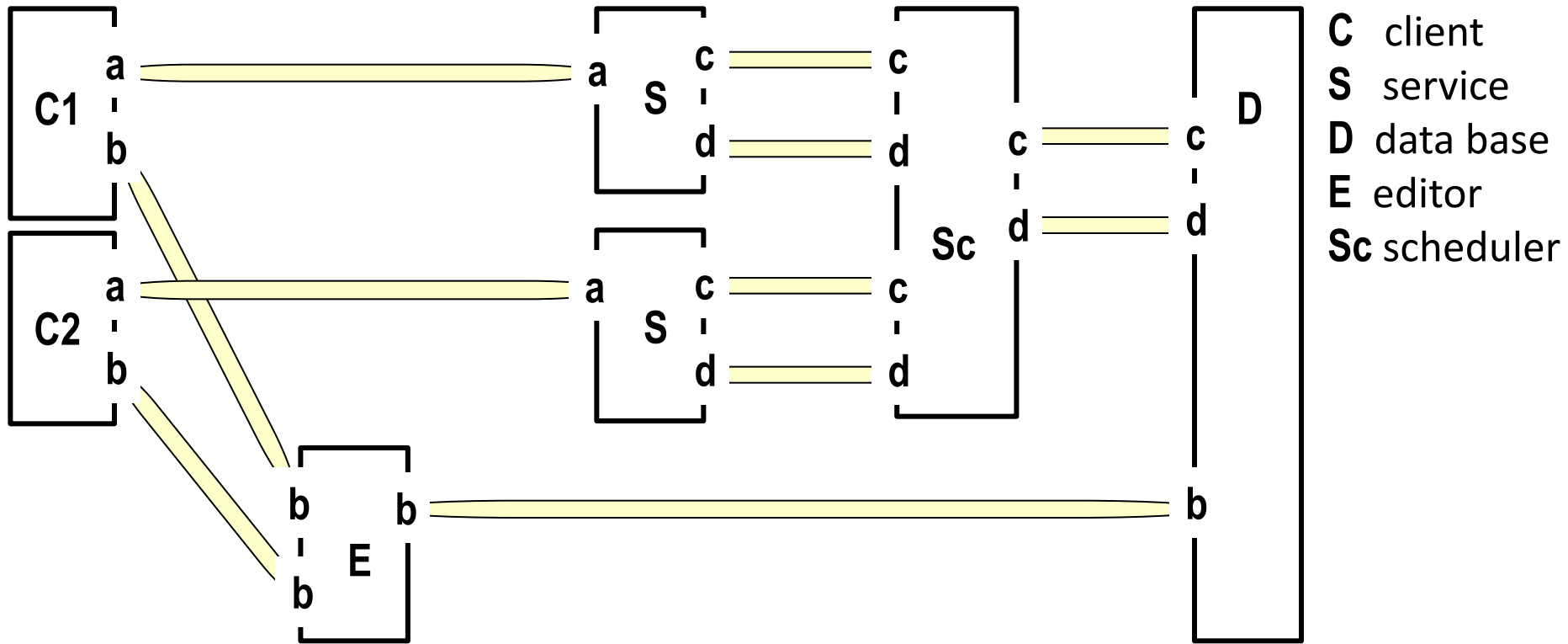
C1 • C2 • S • E • D

a messages from client

b messages to client

c message from service

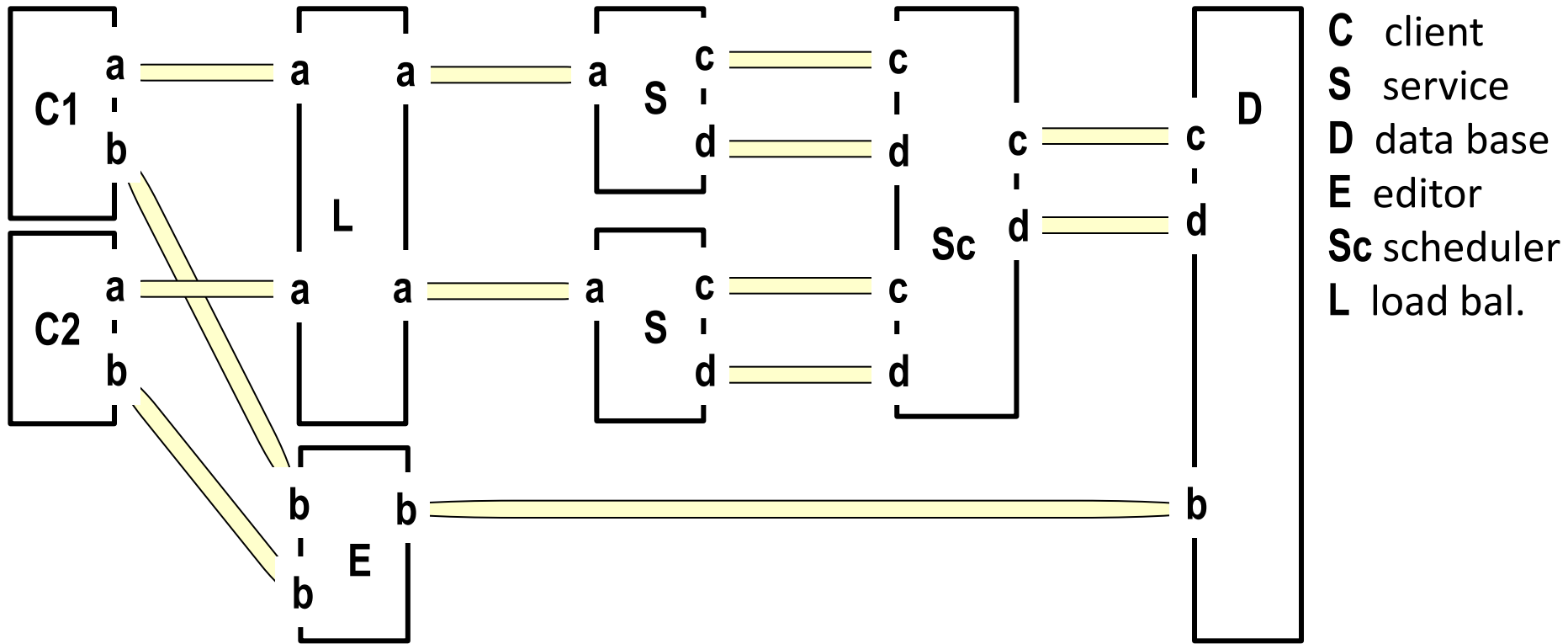
d message to service



C1 • C2 • E • S • S • Sc • D

a messages from client
b messages to client

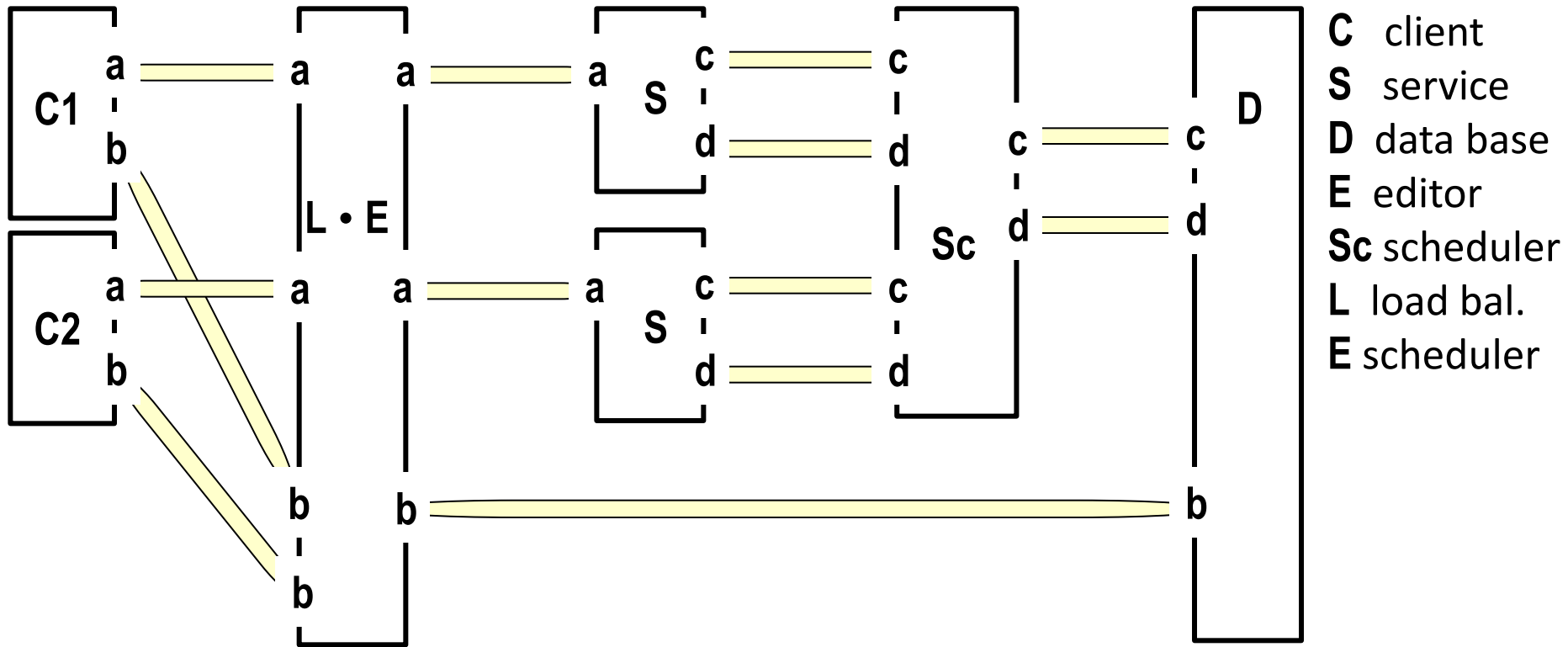
c message from service
d message to service



C1 • C2 • L • E • S • S • Sc • D

a messages from client
b messages to client

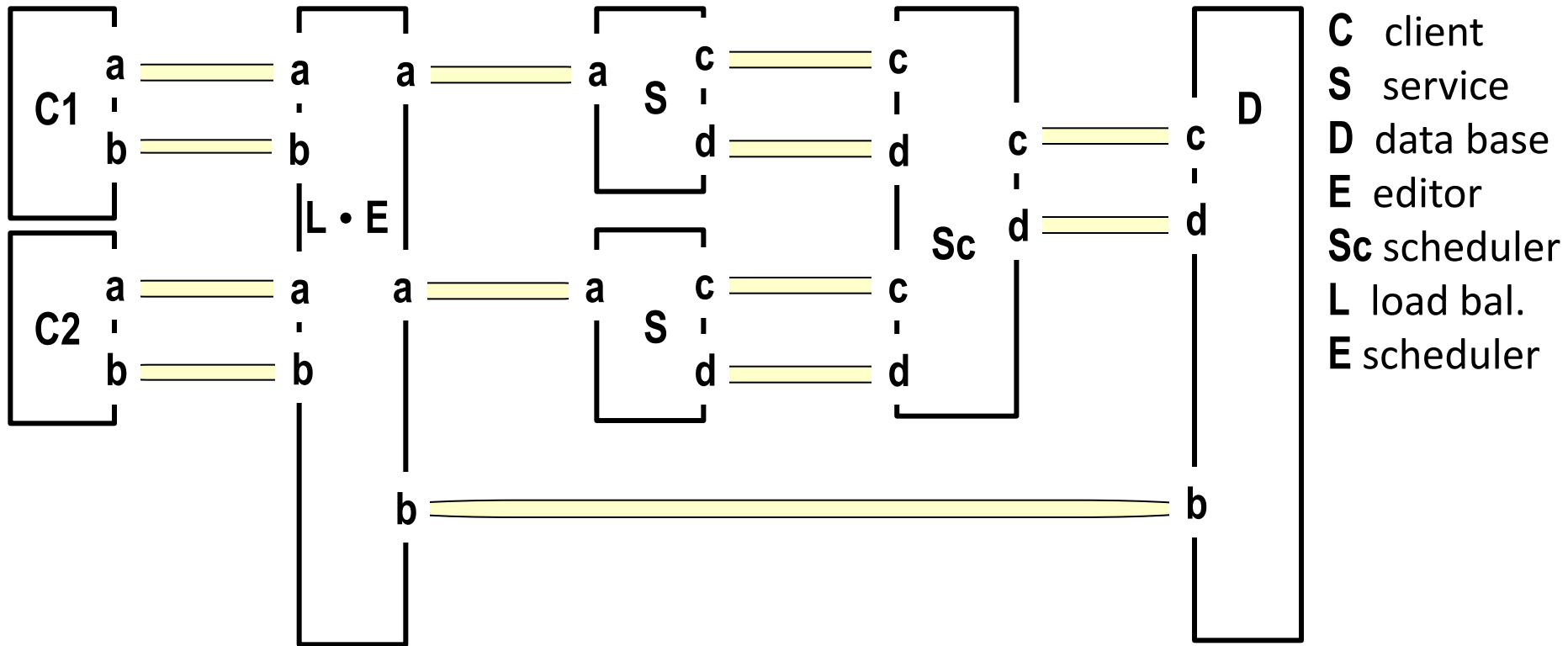
c message from service
d message to service



C1 • C2 • (L • E) • S • S • Sc • D

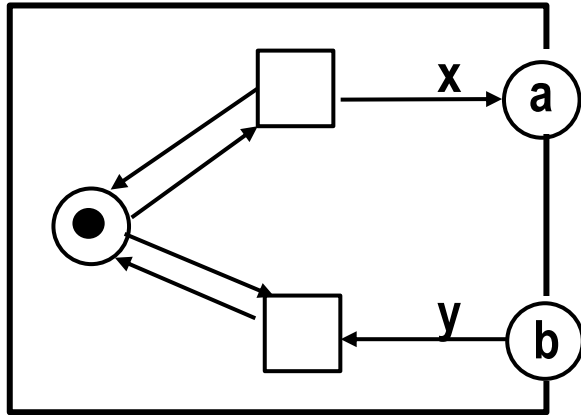
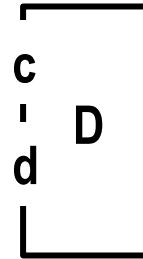
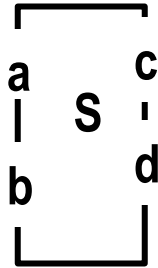
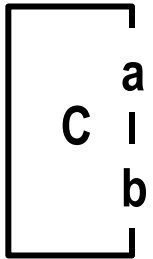
a messages from client
b messages to client

c message from service
d message to service

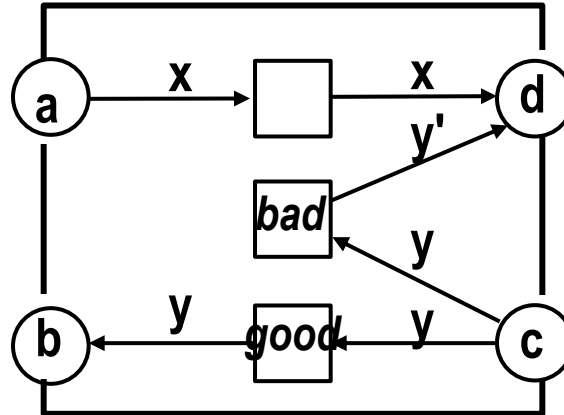


C1 • C2 • (L • E) • S • S • Sc • D

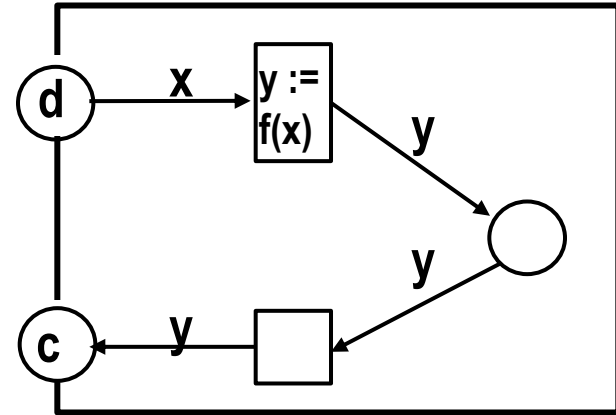
A look inside the components



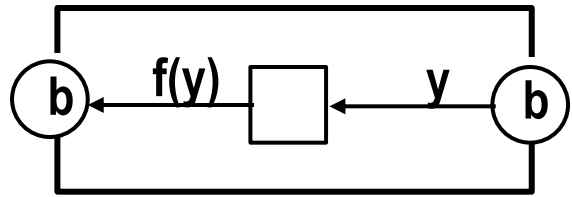
behavior of client **C**



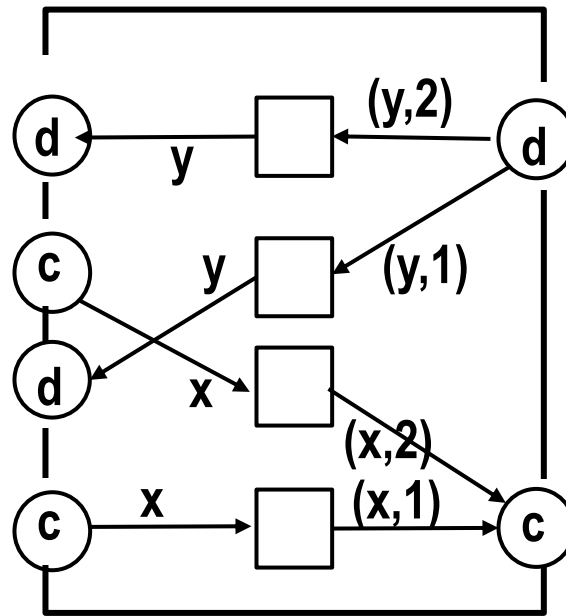
behavior of service **S**



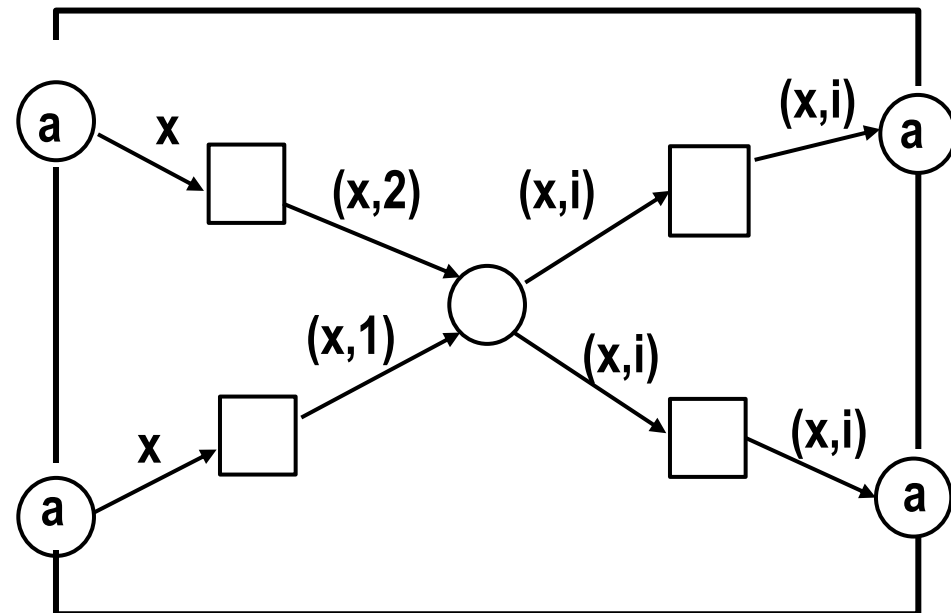
behavior of Data base **D**



behavior editor **E**

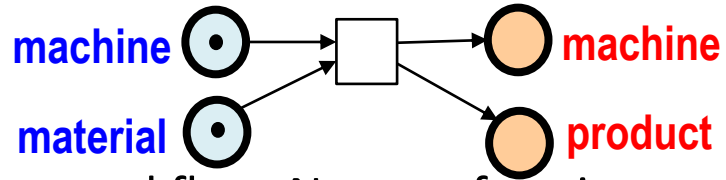


behavior of Scheduler **Sc**



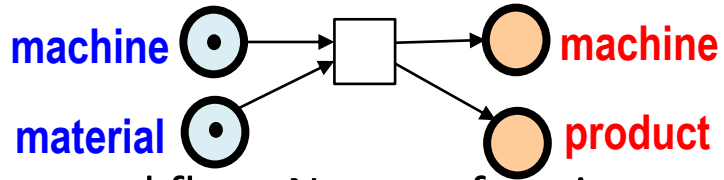
behavior of Load balancer **L**

Multiple labels

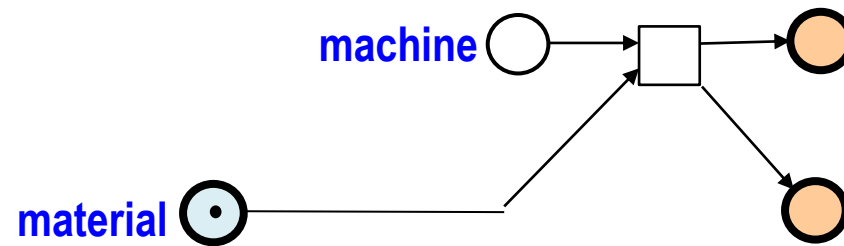
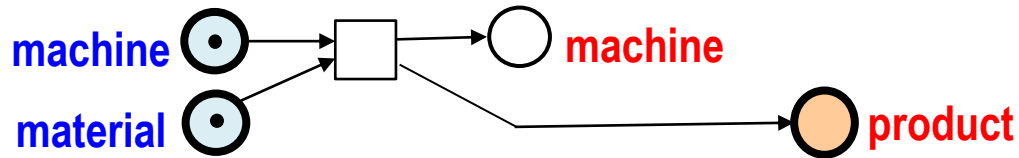


a. workflow N , transforming material into products by help of a machine

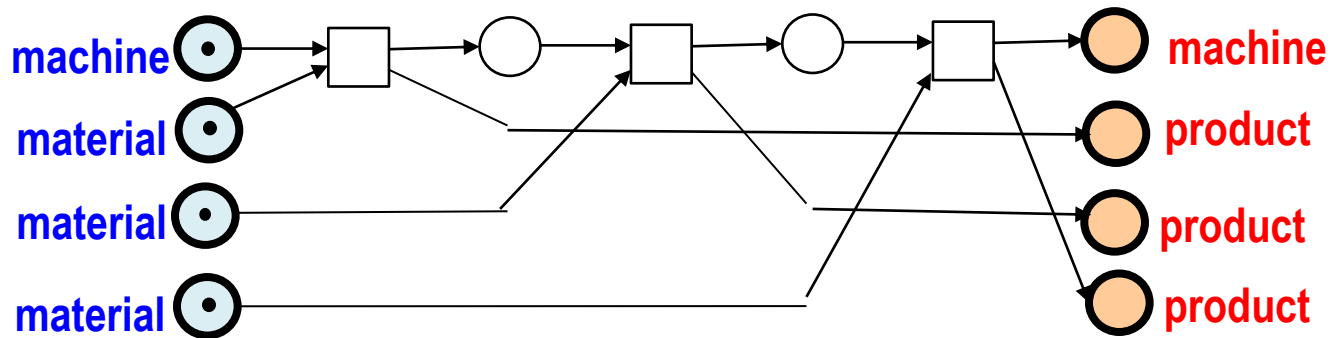
Multiple labels



a. workflow N, transforming material into products by help of a machine



b. composed workflow, $N \bullet N$



c. composed workflow, $N \bullet N \bullet N$

Summing up

Double sided components
are intuitively most natural

customer and *supplier*
provider and *requester*
producer and *consumer*
buy side and *sell side*
input and *output*
required and *offered*

Road map

1. Components and composition:
the basic paradigm for communication
- 2. Fundamental properties of the composition operator**
3. Components' contents
4. ... even more general

Composition is about *architecture*

- strict and formal for the interface
- entirely liberal for the components' contents

Assume a fixed interface alphabet Λ .

Let \mathcal{C} denote the set of components with

- gate labels from Λ and
- empty contents

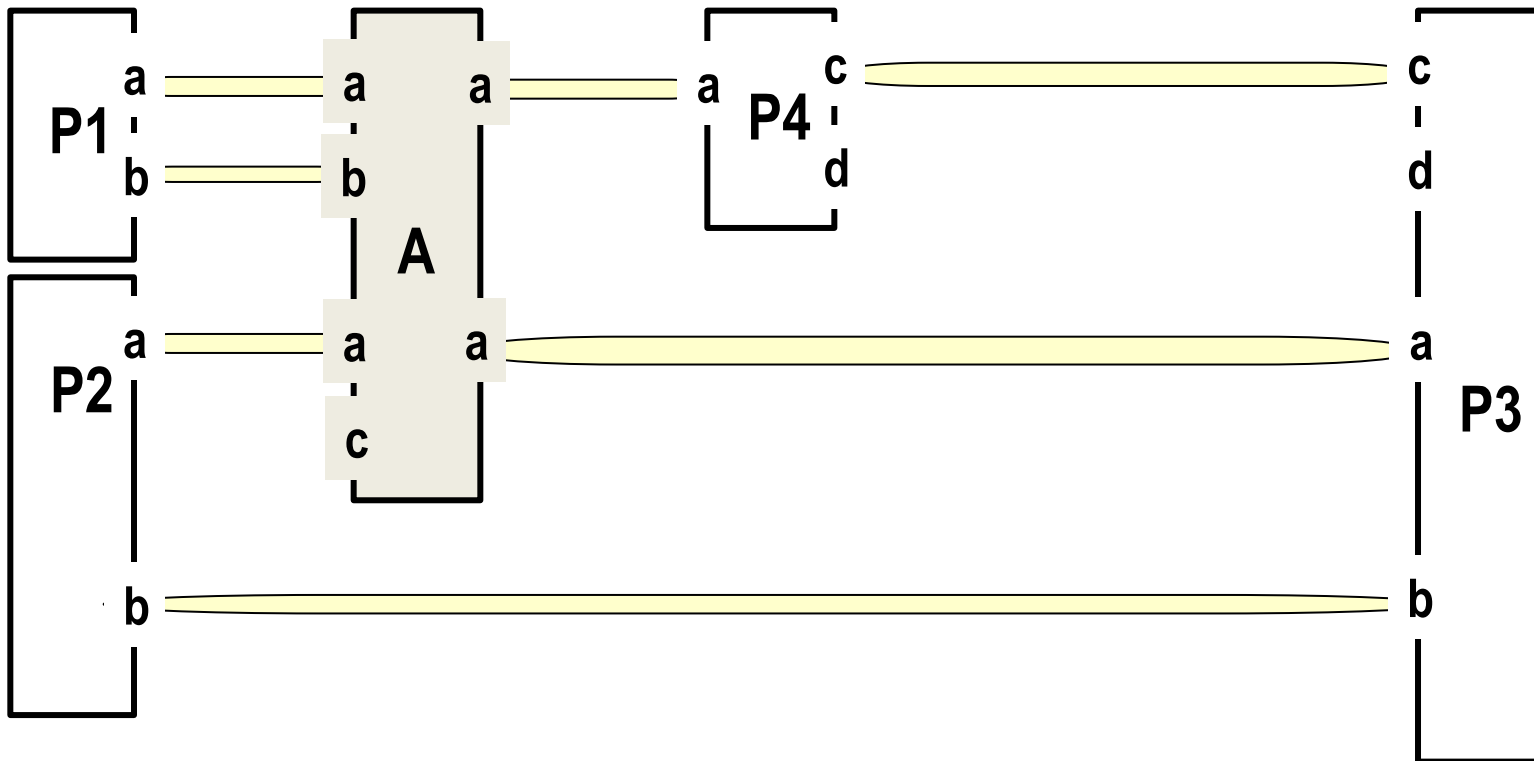
Components' contents: later

Composition on \mathcal{C} is *universal*:

Given *any* finite component network:

Can it be composed from its components?

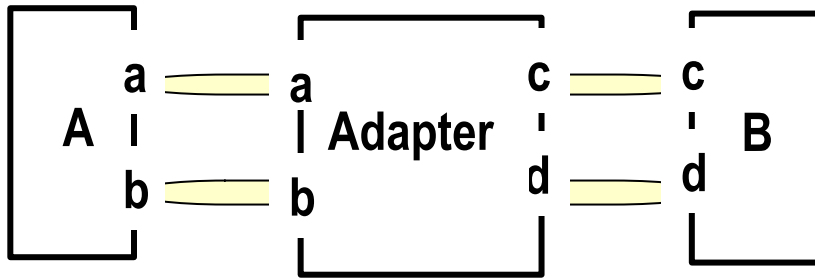
Yes!



P1 • P2 • A • P3 • P4

Composition on \mathcal{C} is *total*

Any two components in \mathcal{C} can be composed.



Want to glue **a** with **c** and **b** with **d**.
New kind of composition?

Composability predicate for **A** and **B**?

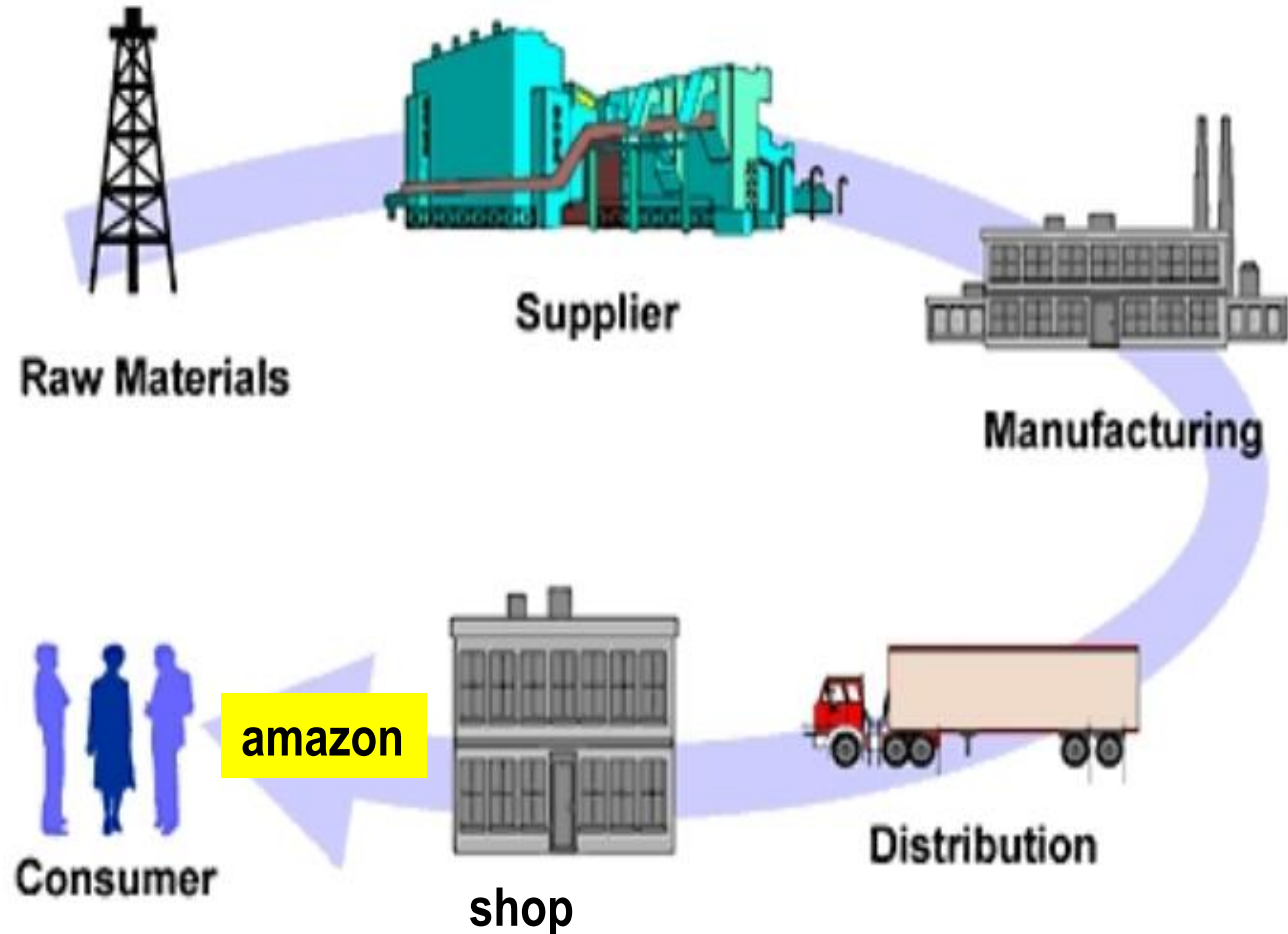
Instead: Construct an adapter, **C**,
internally organizing composition,
and consider **A • C • B**.

One notion of composition
allows a generic,
ultimately simple,
infrastructure.

Composition in \mathcal{C} is *associative*:

$$(A \cdot B) \cdot C = A \cdot (B \cdot C).$$

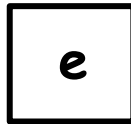
... inevitable for “large”
compositions.



RM • Su • Ma • Di • Sh • Am • Co

Summing up: Composition in \mathcal{C} yields a *monoid*

Observation: \mathcal{C} contains



(it holds: $A \cdot e = e \cdot A = A$)

Hence $(\mathcal{C}; \bullet, e)$ is a *monoid*.

... just as the words over an alphabet!

*This is the second
most beautiful
news in recent days*

A word on commutativity

Def. An operator $+$ on \mathcal{C} is *commutative*

iff for all $A, B \in \mathcal{C}$ holds:

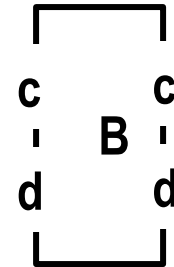
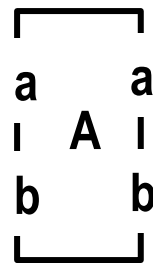
$$A + B = B + A.$$

Observation: \bullet is not commutative

Theorem

$A \bullet B = B \bullet A$ holds

if A and B use disjoint labels.



... but Frank loves commutativity!

Frank, please, don't be so stupid!

Frank uses three services:

Haircut, new passport, border control.



H



P



B

H • P • B

Good!
Bravo!

... but Frank's composition is not commutative!

Frank, please

Frank use

Haircut, no

Commutative composition is a bad idea!



H P

P

P • H • B

Bad!



Road map

1. Components and composition:
the basic paradigm for communication
2. Fundamental properties of the composition operator
- 3. Components' contents**
4. ... even more general

Remember:

Composition is

- strict and formal for the interface
- entirely liberal for the components' contents

Formulate contents (behavior) as you wish!

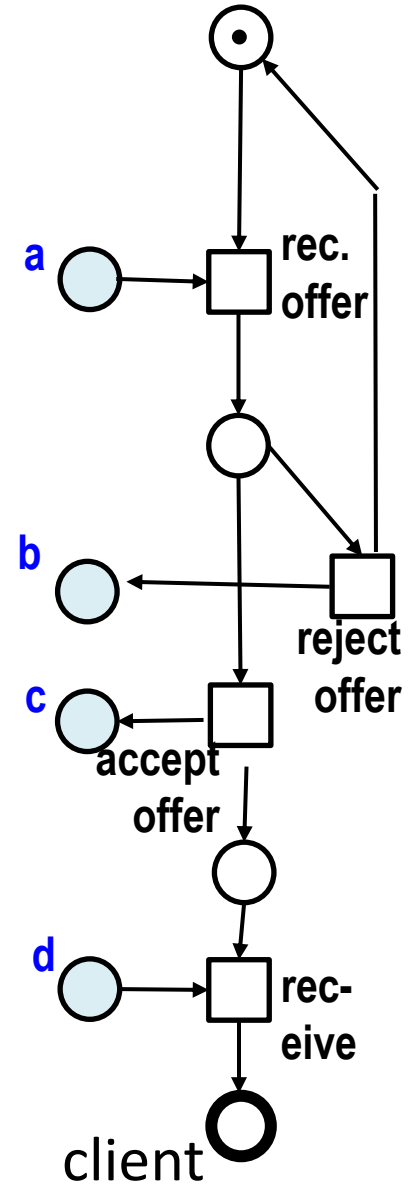
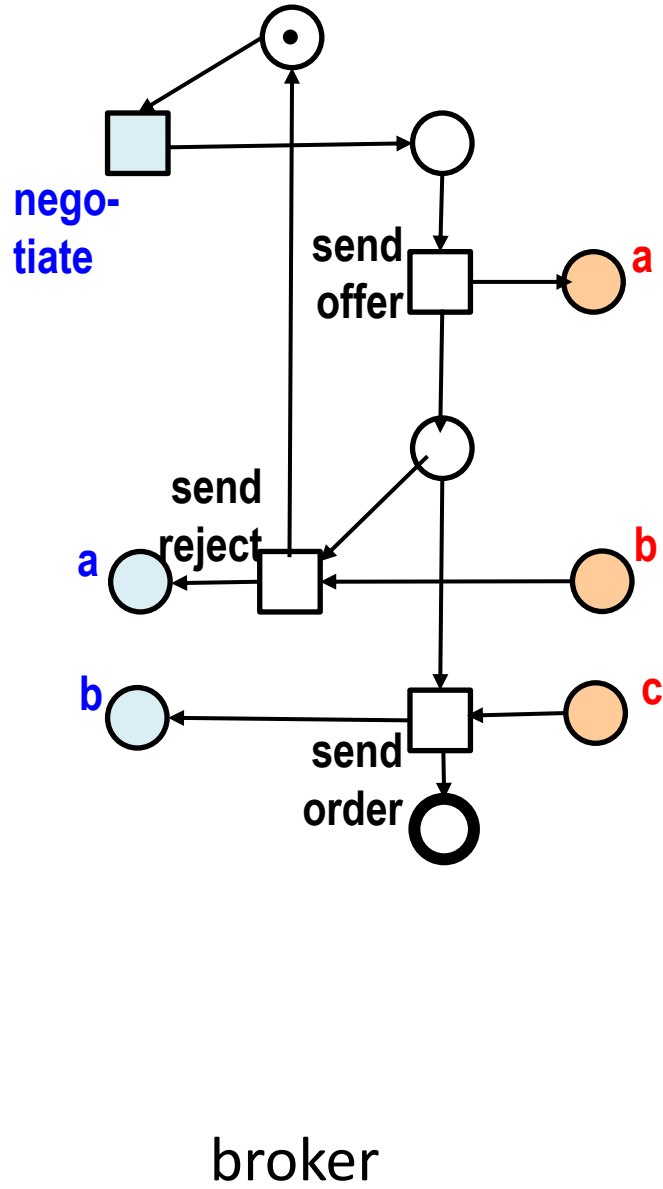
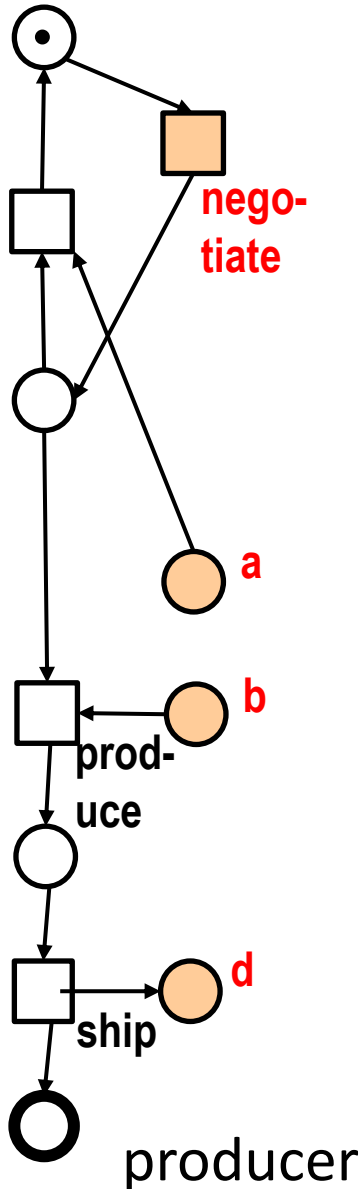
- automata,
- programs,
- π -calculus,
- Petri nets,
- ...

Construct classes \mathcal{D}
of components such that
 $(\mathcal{D}; \bullet, e)$ is a *monoid*.

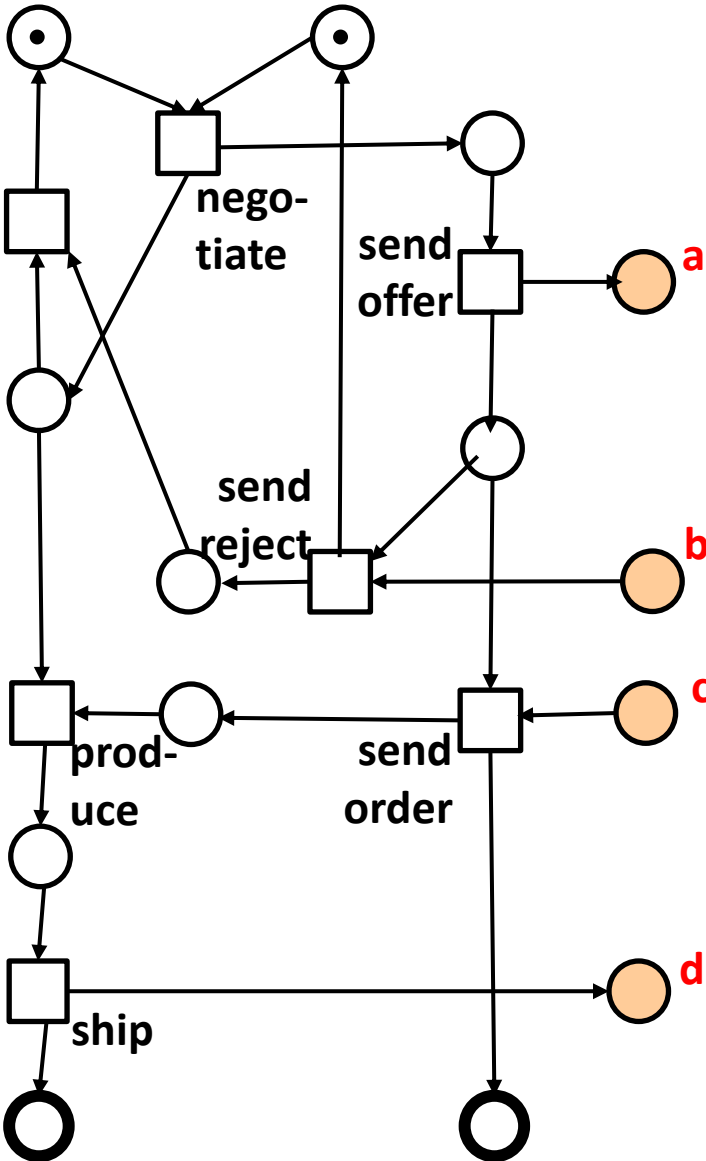
„Instantiations“

The Petri instantiation

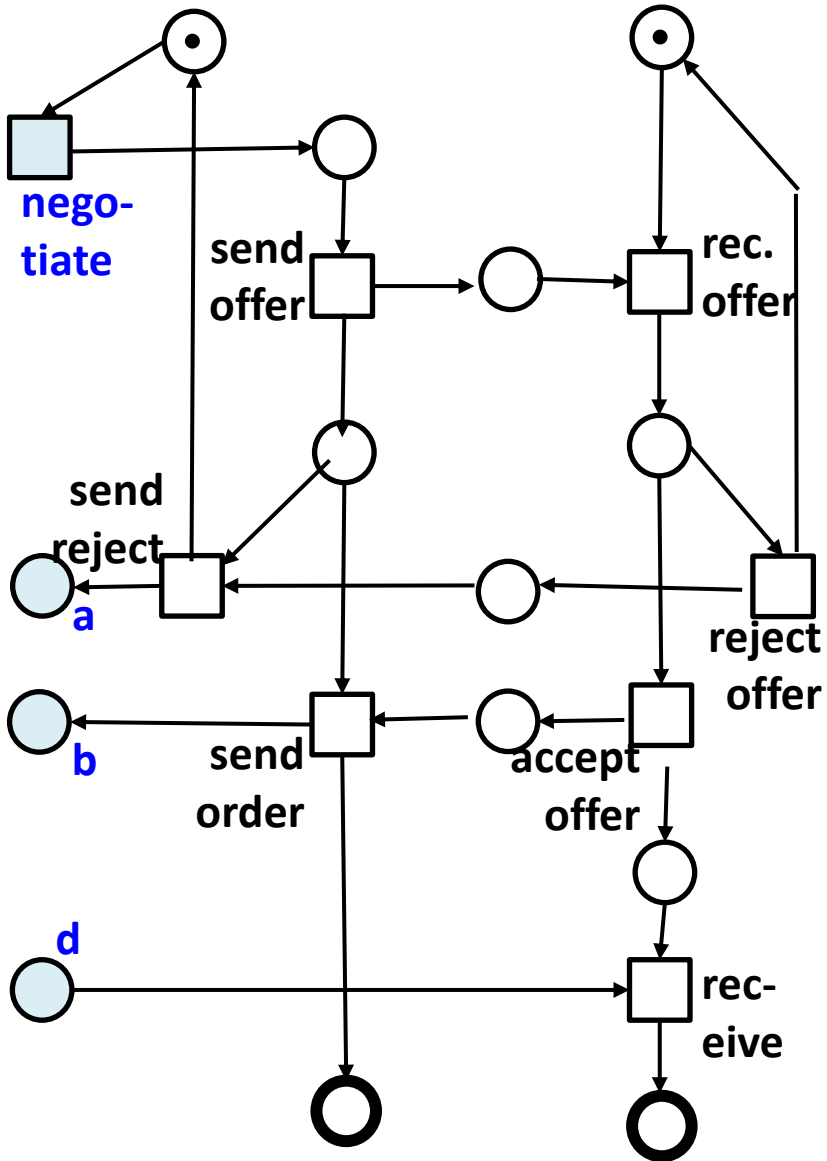
Partition Λ into Λ_P and Λ_T



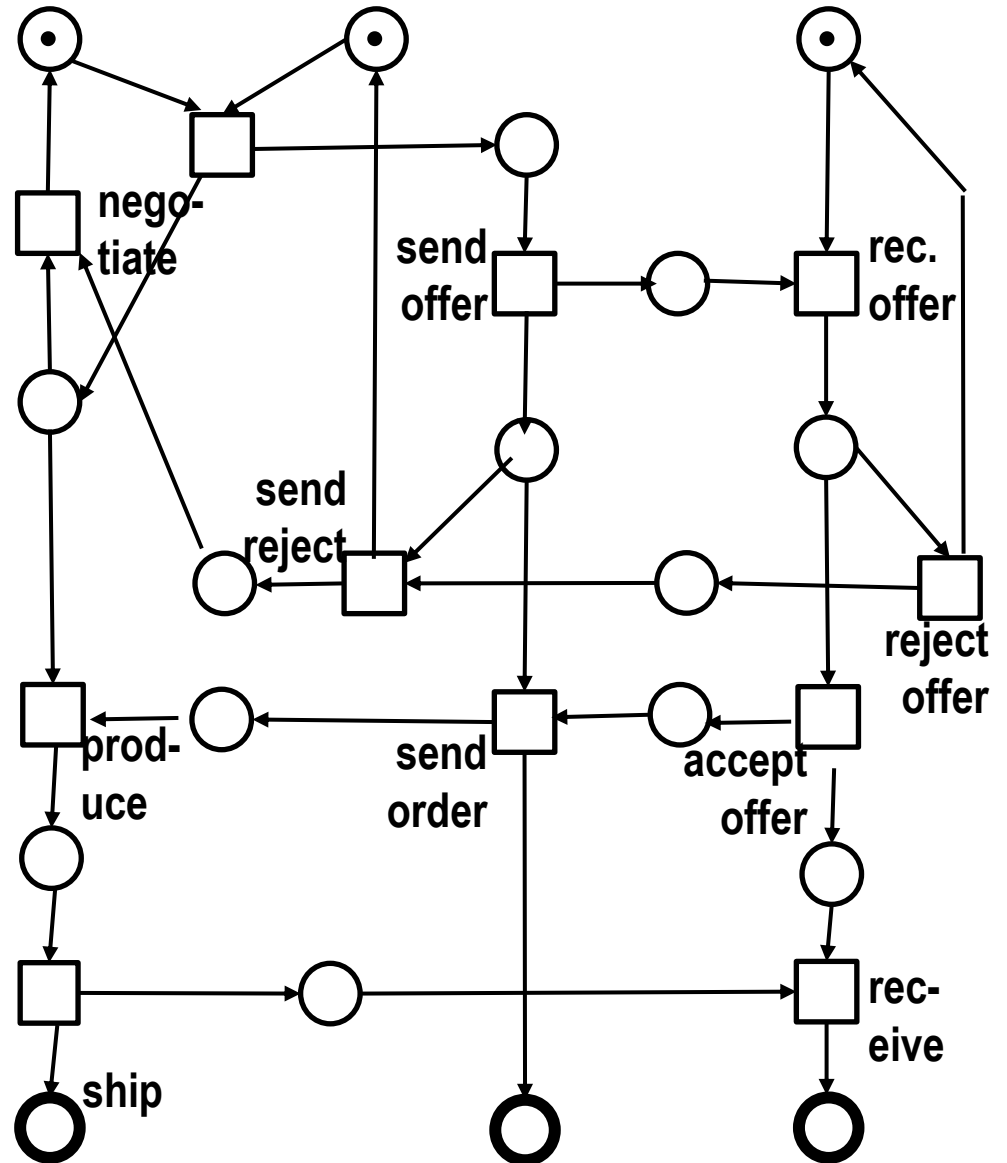
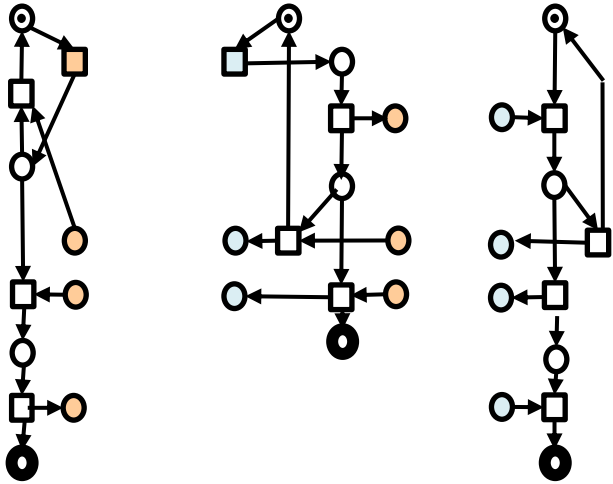
producer • broker



broker • client



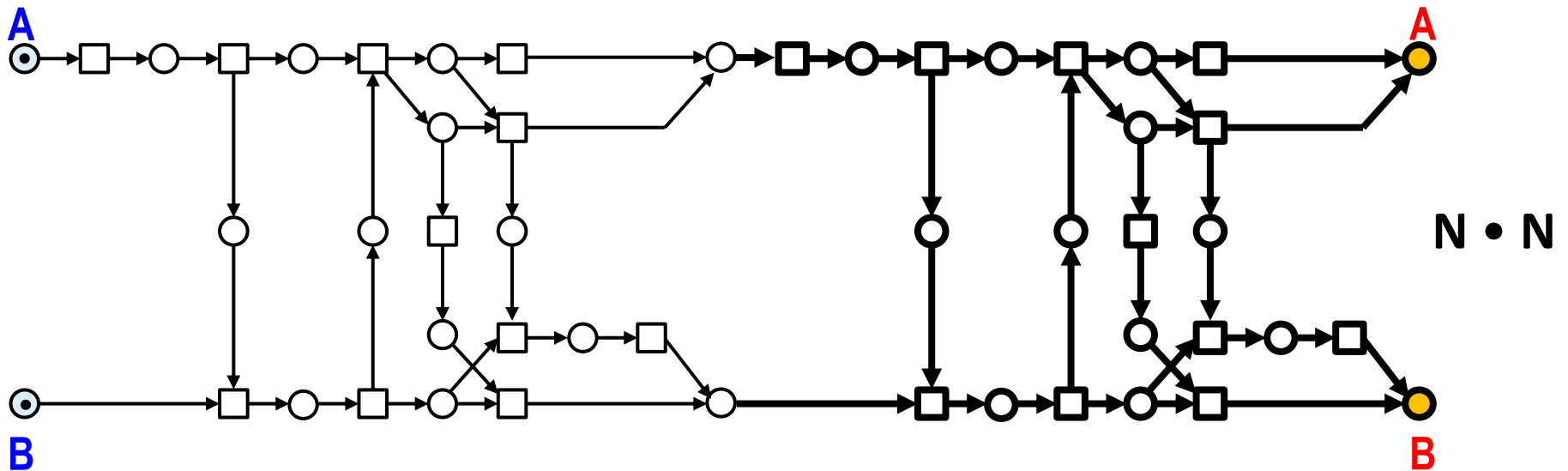
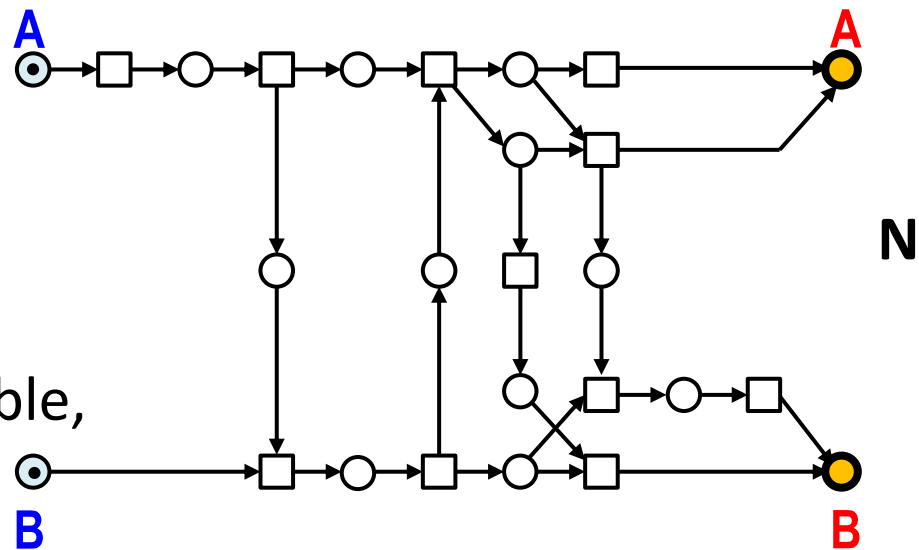
producer • broker • client



The sound WF instantiation

Def: A workflow is *sound* iff

- all its activities are executable,
- the final state is always reachable,
- upon termination, no further tokens remain.

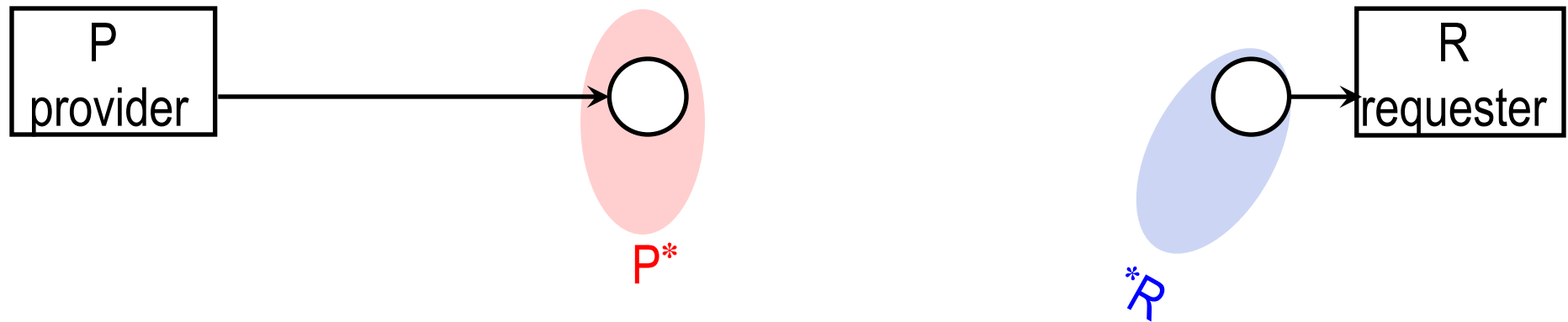


Theorem: Composition of sound workflows is sound.

Road map

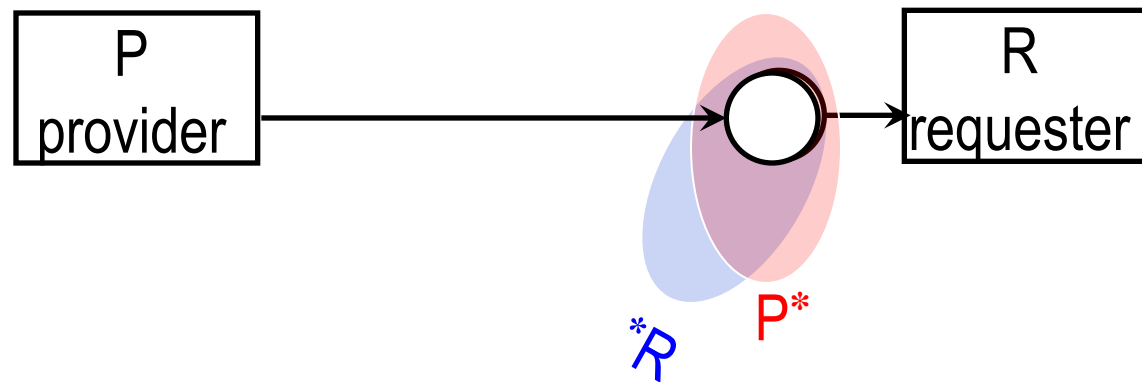
1. Components and composition:
the basic paradigm for communication
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3. Components' contents
- 4. ... even more general**

Right and left interface may overlap!



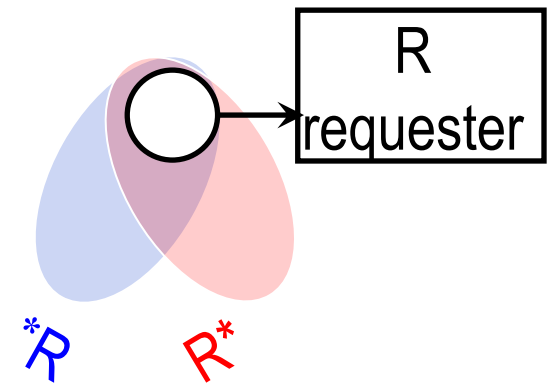
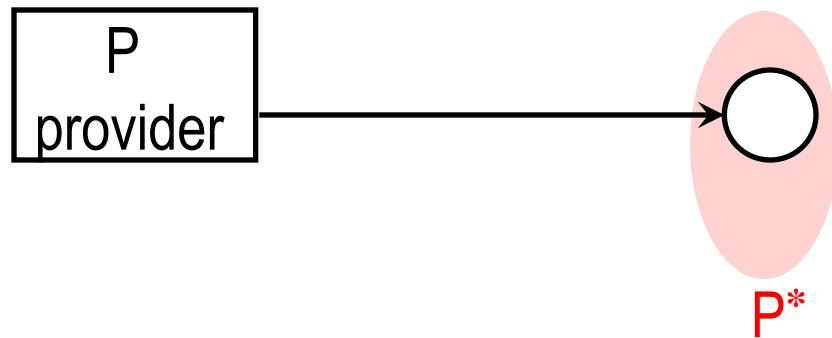
exclusive requester

a variant:

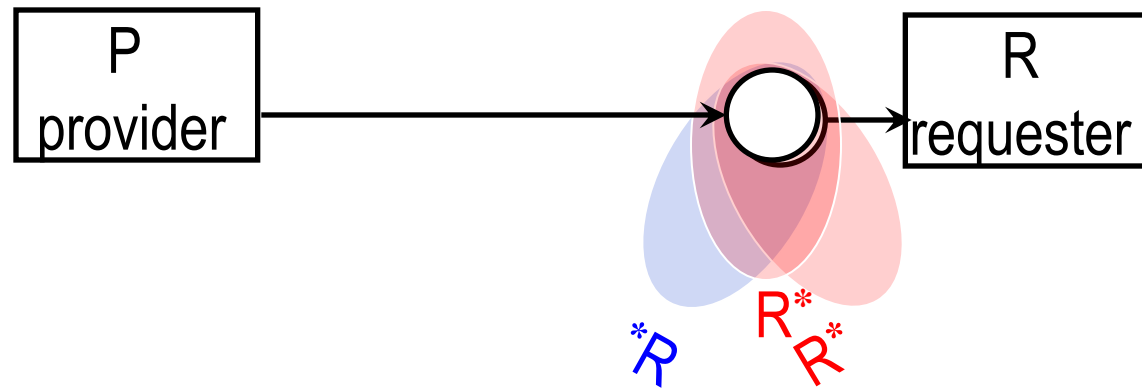


overlapping ports

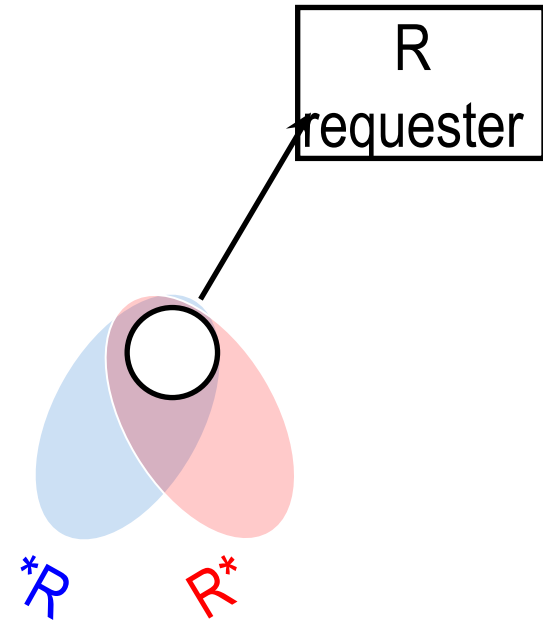
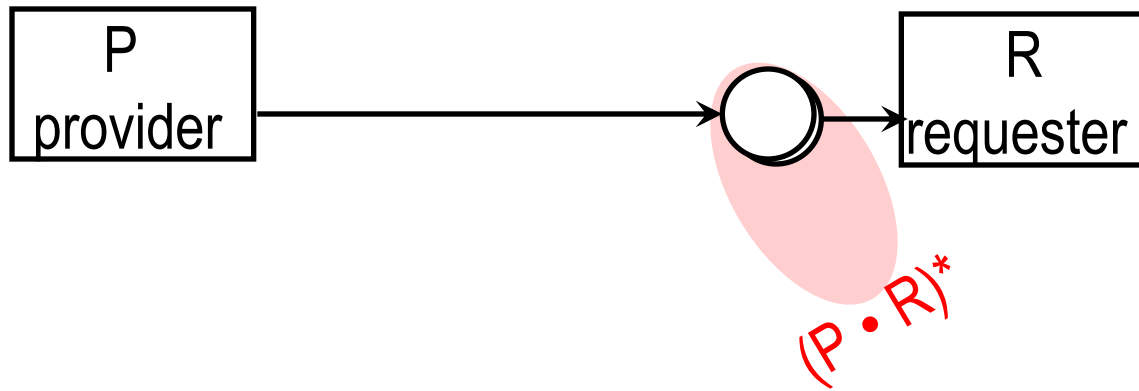
a variant:



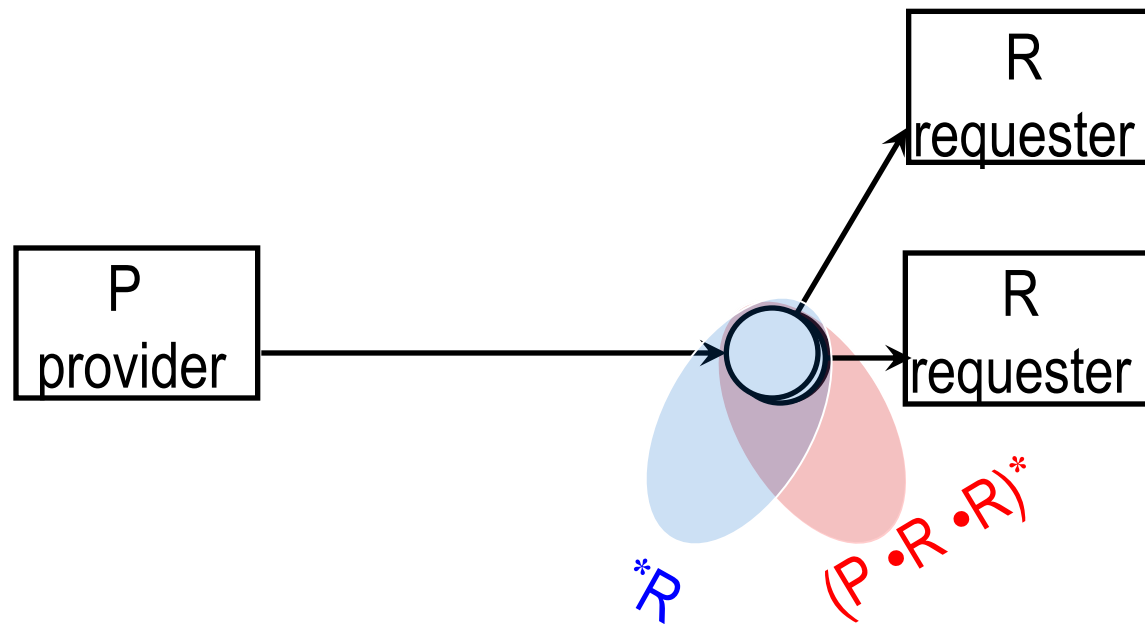
sharing requester



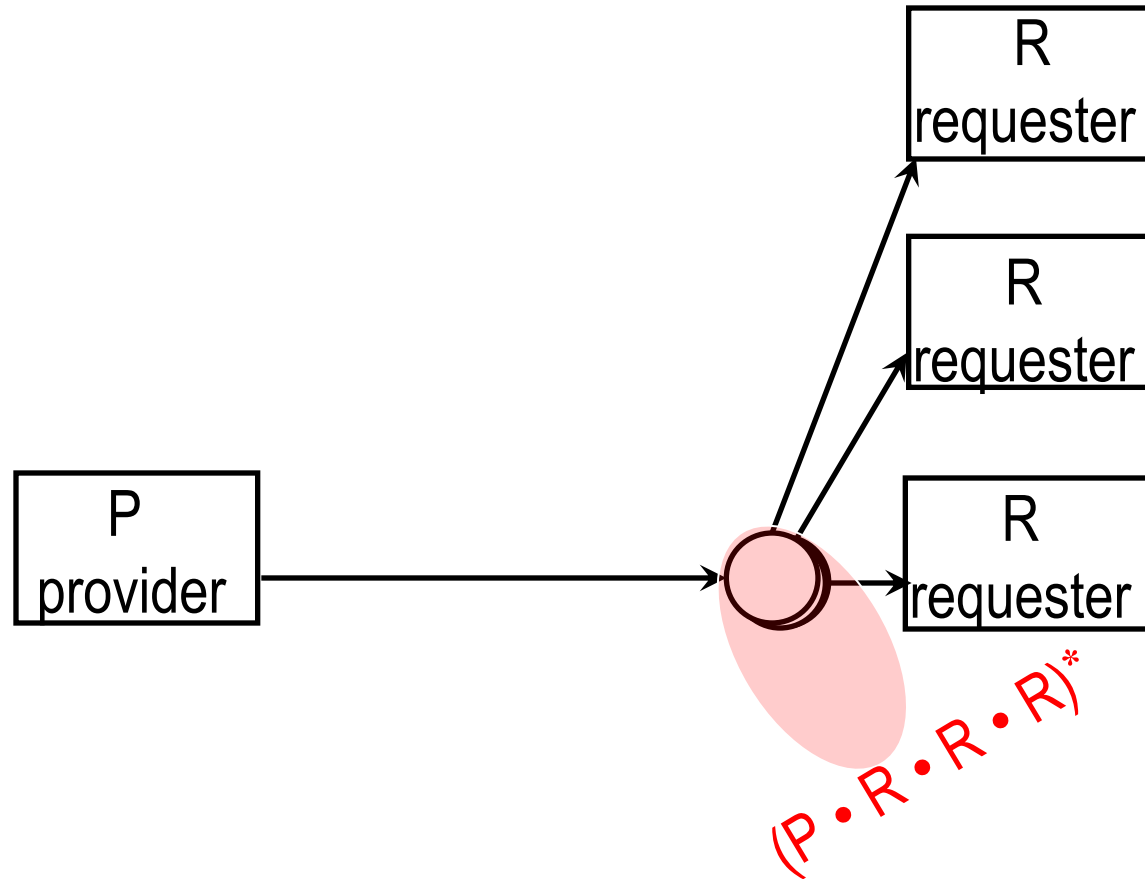
second requester



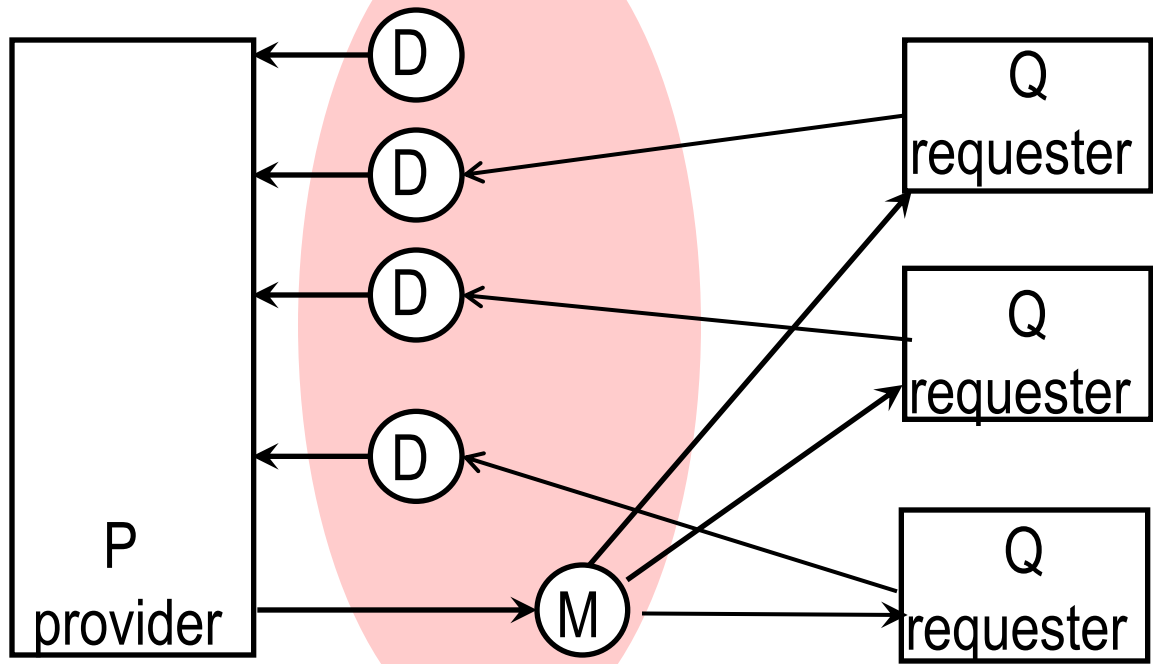
second sharing requester



third requester



more involved requester

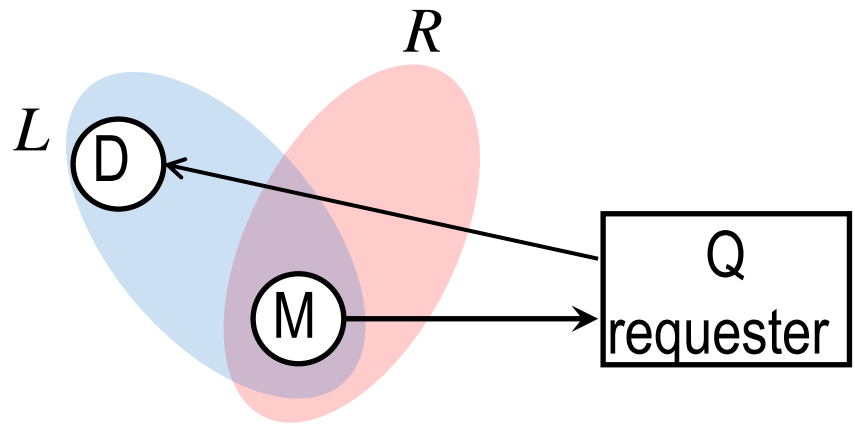


$P \cdot Q \cdot Q \cdot Q$

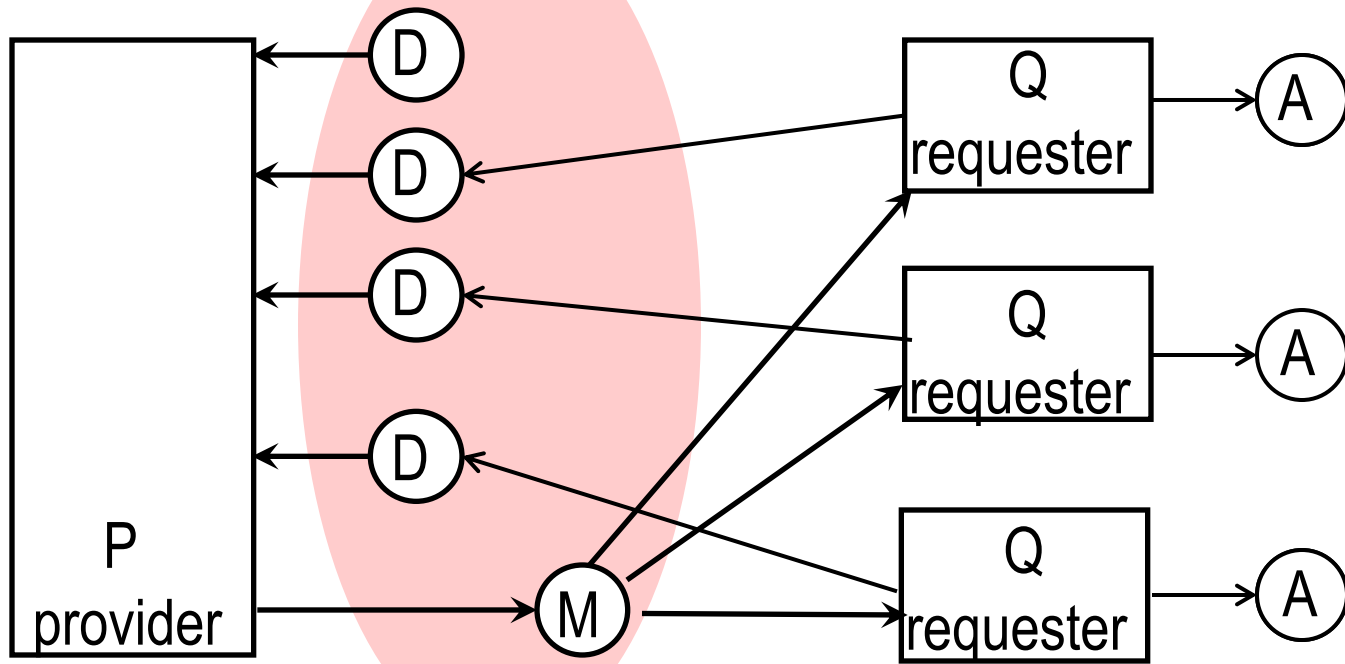
$P \cdot Q \cdot Q$

$P \cdot Q$

generic requester Q :



prefer *this* variant?

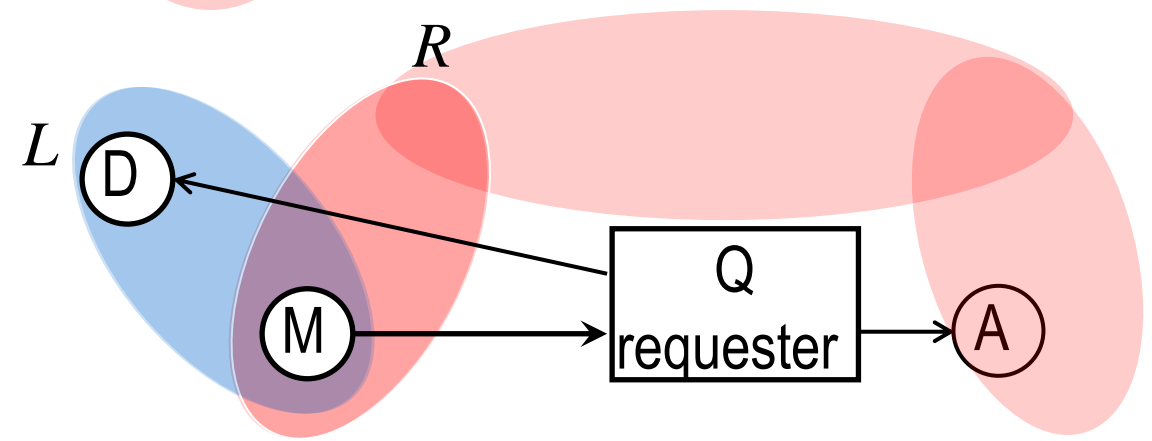


$P \cdot Q \cdot Q \cdot Q$

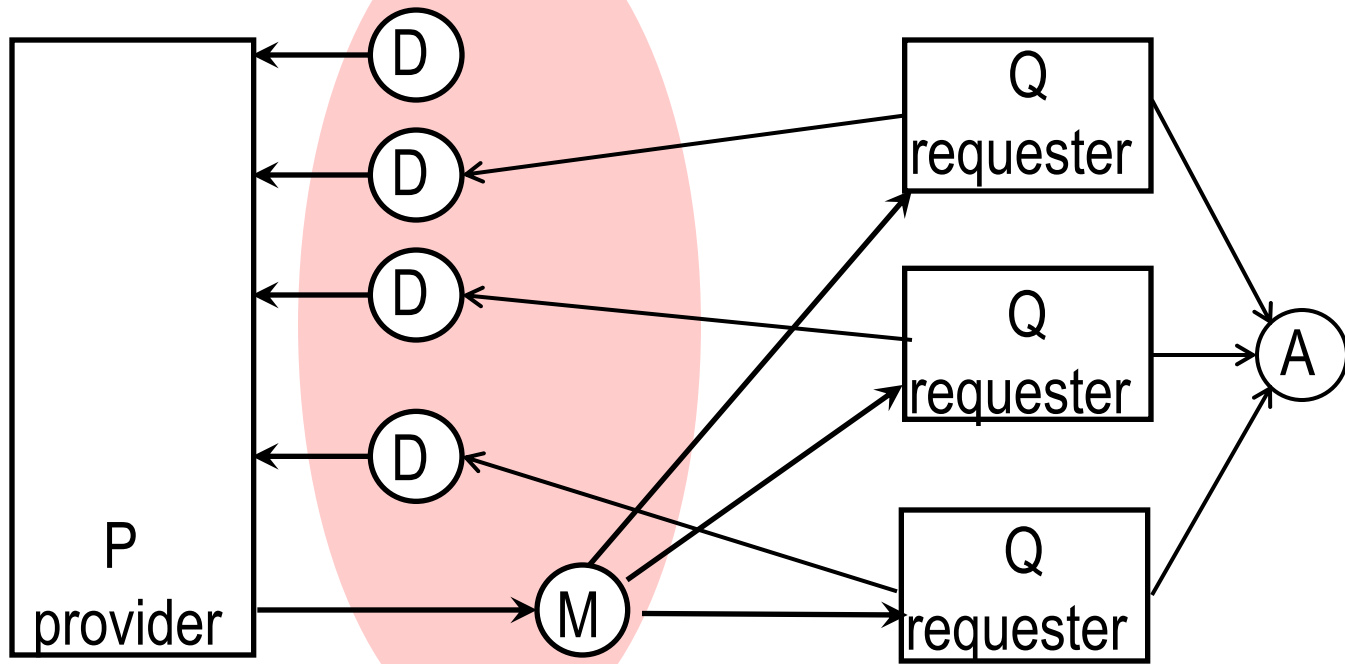
$P \cdot Q \cdot Q$

$P \cdot Q$

generic requester Q :



prefer *this* variant?

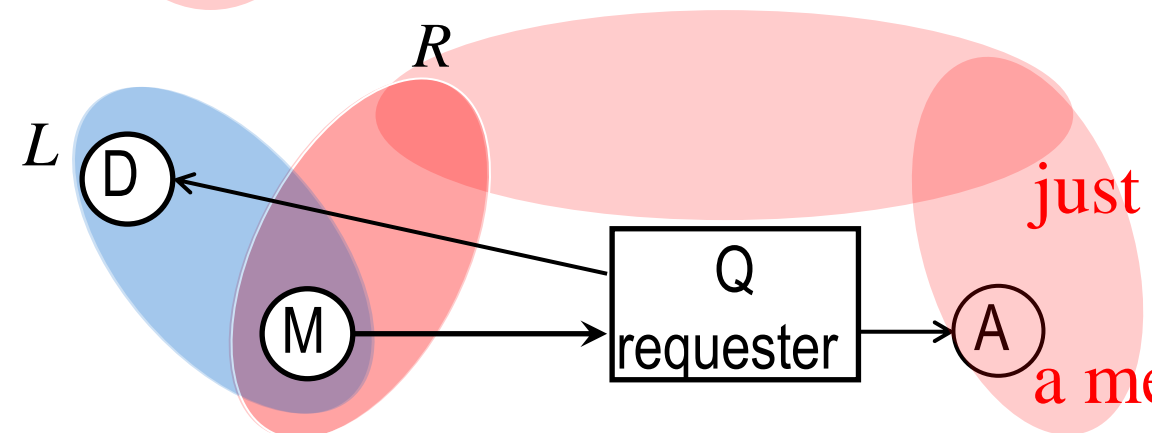


$P \cdot Q \cdot Q \cdot Q$

$P \cdot Q \cdot Q$

$P \cdot Q$

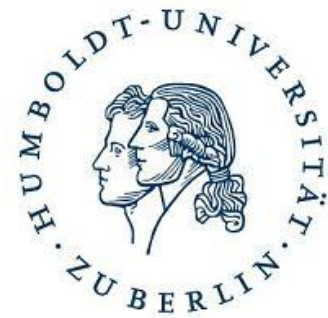
generic requester Q :



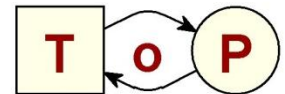
just make
←
a member of *L*

SUMMERSOC

Hersonissos, Wednesday, June 27, 2018. 9.30 – 10.30



Conceptual Fundamentals of Reactive Systems



Theory of
Programming

Prof. Dr. W. Reisig

Wolfgang Reisig

Humboldt-Universität zu Berlin