### SummerSOC 2025

♀ Crete, Greece

# Uncertainty-Aware Machine Learning for Astronomical Data Analysis

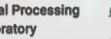
Gregory Tsagkatakis

Institute of Computer Science, FORTH Computer Science Department, University of Crete















Funded by the European Union

### SPL at a glance

### 2006

4 Researchers/Academics (permanent) **1** Postdoctoral Researchers **12** Postgraduate Students 2 Research Engineers





### **Collaborators & Funding**



**Panos Tsakalides Signal Processing lab** FORTH



**CALCHAS** 

Computational Intelligence for Multi-

Source Remote Sensing Data Analytics

TITAN ARTIFICIAL INTELLIGENCE IN ASTROPHYSICS



MARIE CURIE ACTIONS

European

Commission



Jean-Luc Starck **CosmoStat lab CEA**, **France** 

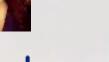


Mahta Moghaddam MiXIL lab USC







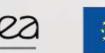


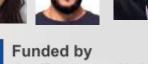
Signal Processing



**c**esa

NASA





Horizon 2020

fellenic Foundation f

European Union funding

for Research & Innovation

the European Union 3



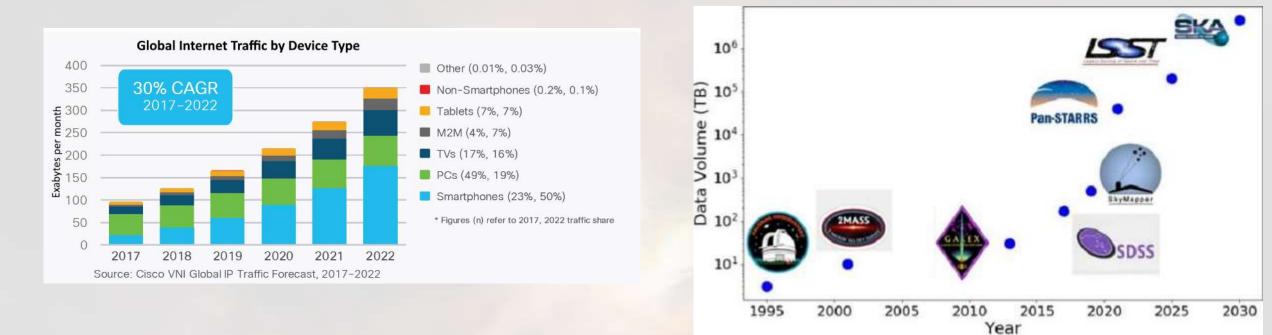








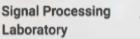
# **The Big Data Revolution**









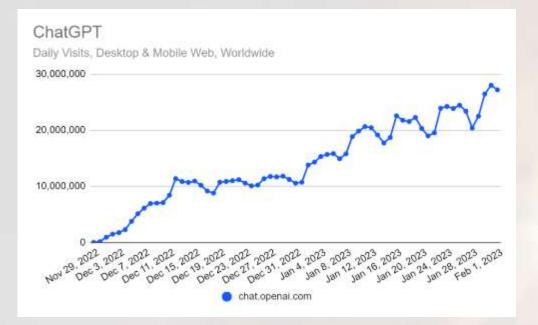


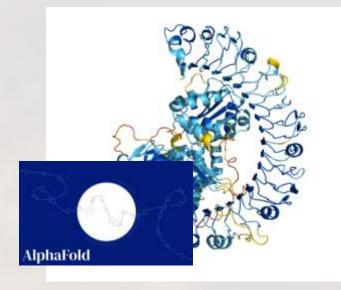


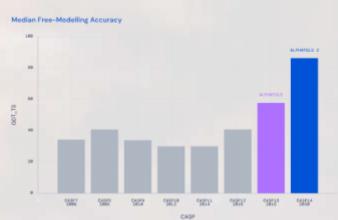




# **The AI Revolution**







Jumper, John, et al. "Highly accurate protein structure prediction with AlphaFold." Nature. 2021.







Signal Processing



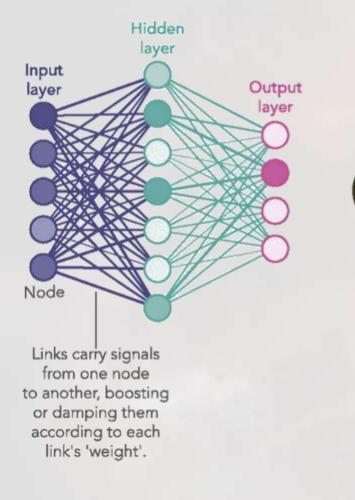


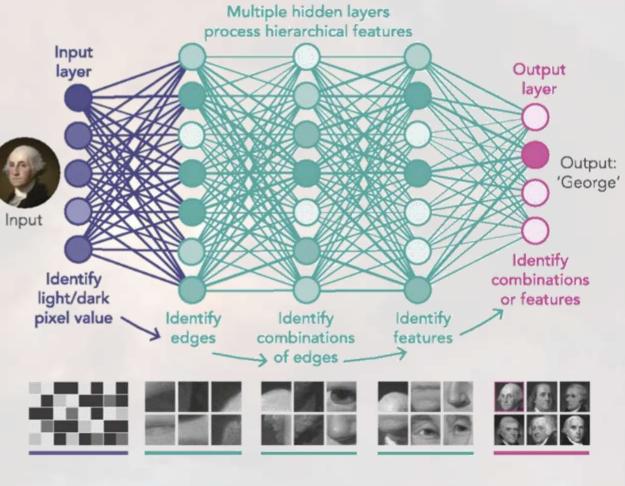


### **Deep Learning**

1980S-ERA NEURAL NETWORK









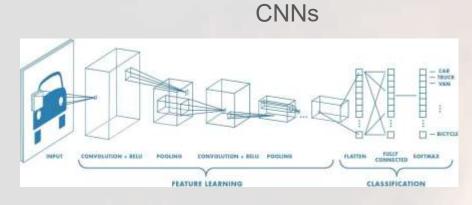


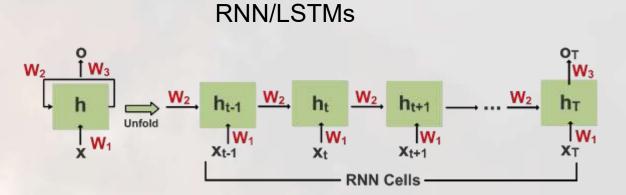
Signal Processing Laboratory

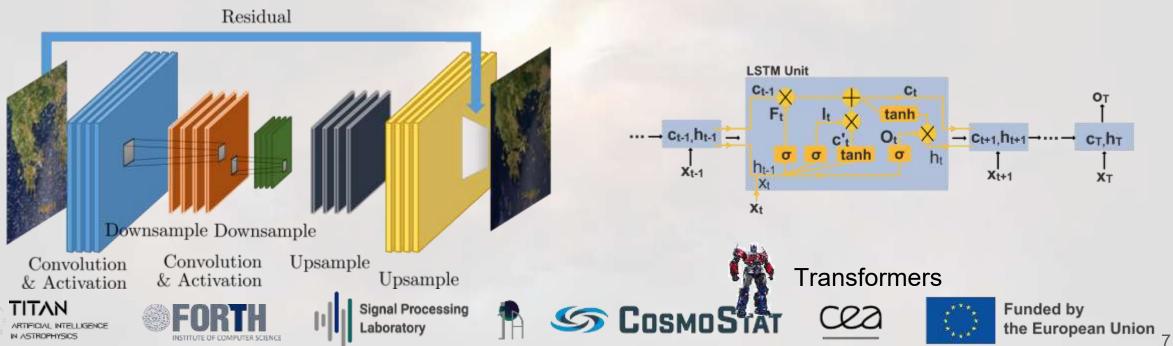




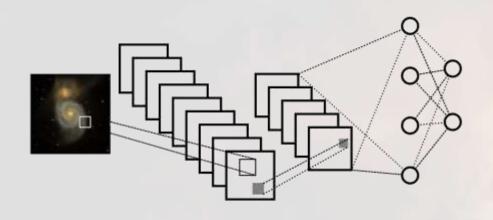
### **State-of-the-art in DL**

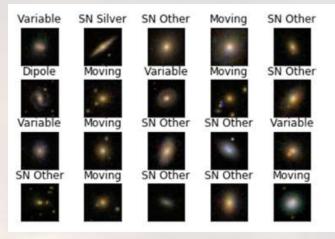






### **Deep Learning in Astronomy**

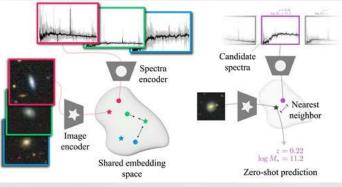




Input Image

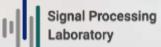
Convolution Layer Max-pooling Fully Connected Layer

















# **Uncertainty (model)**





alaskan malamute





siberian husky



siberian husky

Epistemic Uncertainty:

Due to lack of knowledge about a system or process.

Can be reduced as more knowledge is gained.















# **Uncertainty (data)**





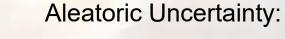




cat







- inherent randomness in a system or process (flipping a coin
- cannot be reduced with more information or knowledge about the system.







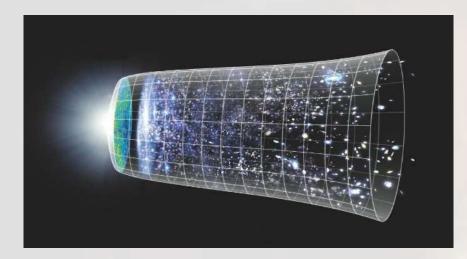
Signal Processing Laboratory

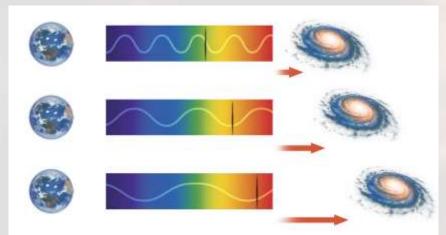






### **Redshift estimation**





# Telescopes with infrared detectors allow us to see the ancient light of the first galaxies, which has been relishifted over space and time. HUBBLE'S LIMIT THE FAST WEBB'S LIMIT THE BIO BAND







Signal Processing Laboratory

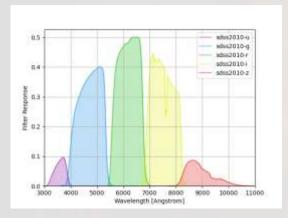






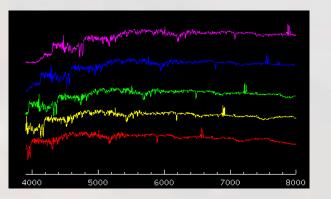
Funded by the European Union 11

# **Observations for Redshift estimation**



### Photometric

- > 3-4 broad bands
- ➤ Cheap
- ➢ Inaccurate

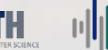


### Spectroscopic

- Extended spectral range
- $\succ$  Expensive
- Accurate





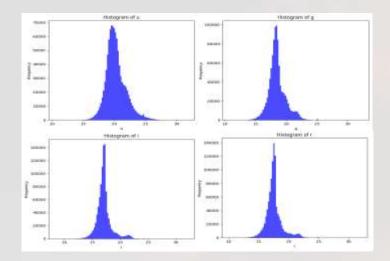


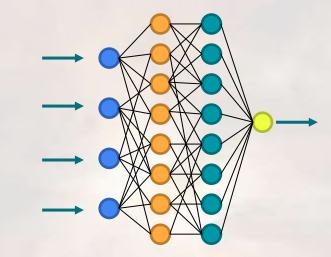
Signal Processing Laboratory

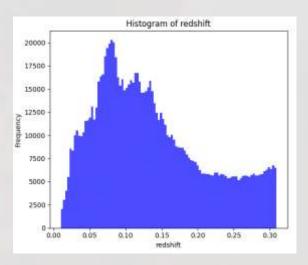




### **ANNs for Photometric Redshift Estimation**



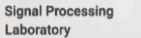
















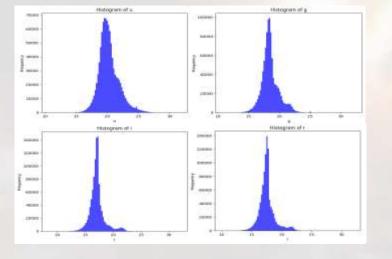
### **ANN - Regression**

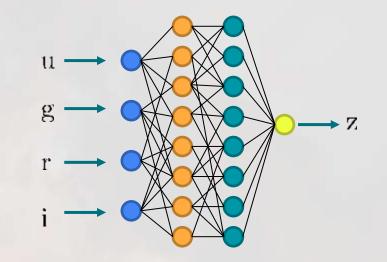
Baseline regression model  $\hat{y}_i = f(x_i; \mathbf{w})$  where:

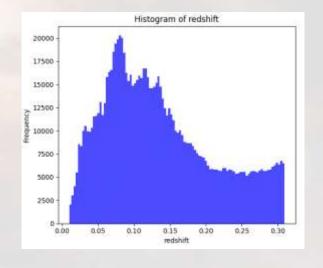
- $f(x_i; \mathbf{w})$  is the prediction for the *i*-th observation,
- $y_i$  is the actual value for the *i*-th observation

Loss function: MSE =  $\frac{1}{n} \sum_{i=1}^{n} (f(x_i; \mathbf{w}) - y_i)^2$ 









Training: 800K Testing: 200K





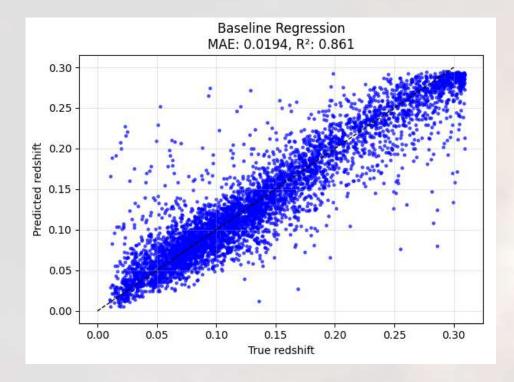


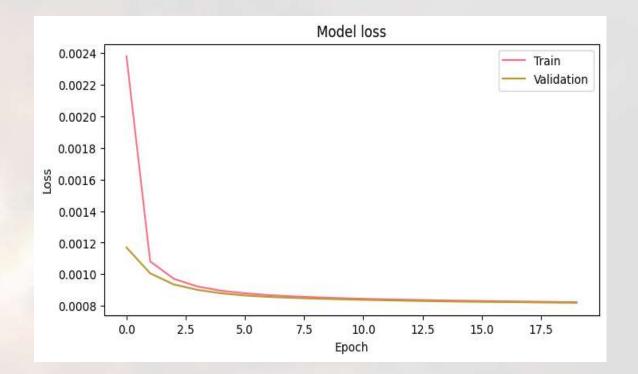
Signal Processing Laboratory





# **Baseline model & Data**











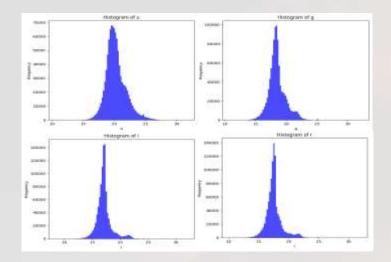
Signal Processing Laboratory

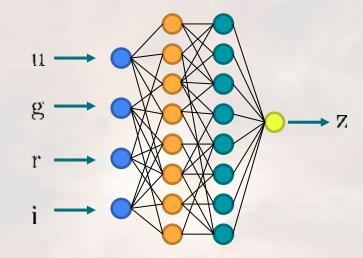


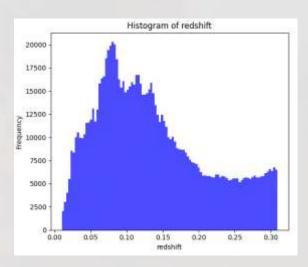




### **Uncertainties**



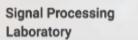










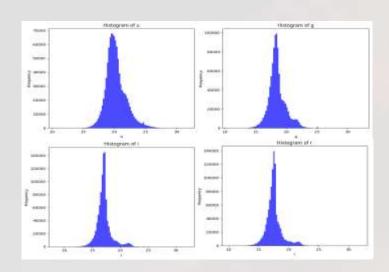


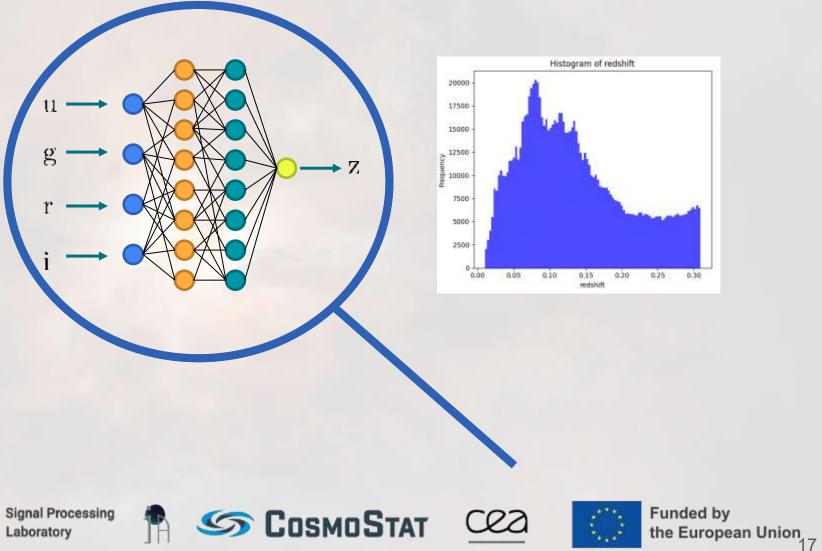






### **Uncertainties (model)**





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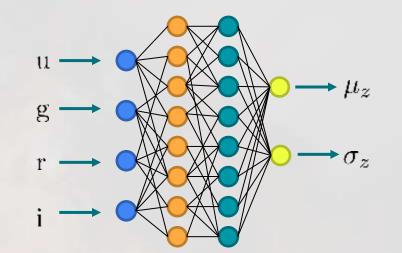
Laboratory



### **Gaussian Regression via ANN**

- The target variable  $y_i \sim \mathcal{N}(f(x_i; \mathbf{w}), \sigma^2)$
- The likelihood for each observation is:

$$p(y_i \mid x_i, \mathbf{w}) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(y_i - f(x_i; \mathbf{w}))^2}{2\sigma^2}\right)$$

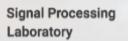


**Loss**: Negative Log-Likelihood (NLL) for N observations is:

$$\mathcal{L}(\mathbf{w}) = -\sum_{i=1}^{N} \log p(y_i \mid x_i; \mathbf{w})$$
$$= \frac{N}{2} \log(2\pi\sigma^2) + \frac{1}{2\sigma^2} \sum_{i=1}^{N} (y_i - f(x_i; \mathbf{w}))^2$$



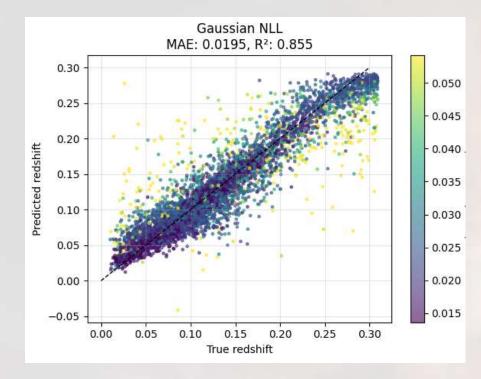


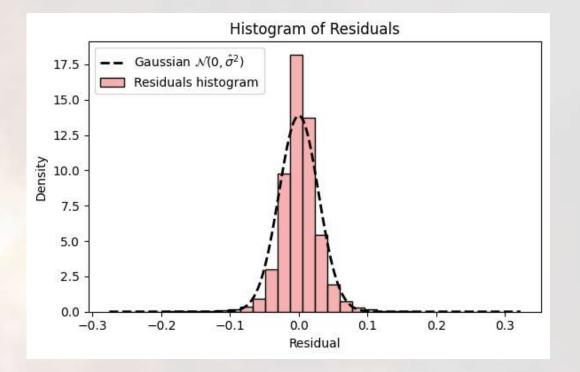






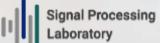
### **Gaussian Regression via ANN**















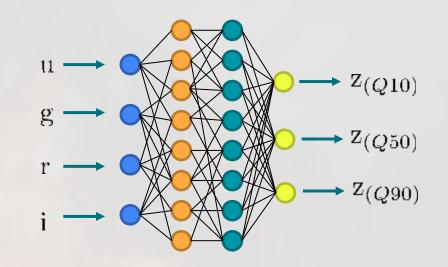


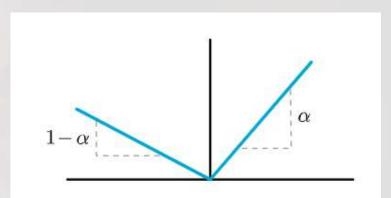


# **Quantile Regression**

- Assume a set of target quantiles  $\{\alpha_k\}_{k=1}^K$ .
- $\hat{\mathbf{y}}_i = f(x_i; \mathbf{w}) = \left(\hat{y}_{i,\alpha_1}, \, \hat{y}_{i,\alpha_2}, \, \dots, \, \hat{y}_{i,\alpha_K}\right)$
- Mean pinball loss (n samples, K quantiles):

$$L_{\alpha}(y, f(x)) = \begin{cases} \alpha |y - f(x)|, & y \ge f(x), \\ (1 - \alpha) |y - f(x)|, & y < f(x). \end{cases}$$









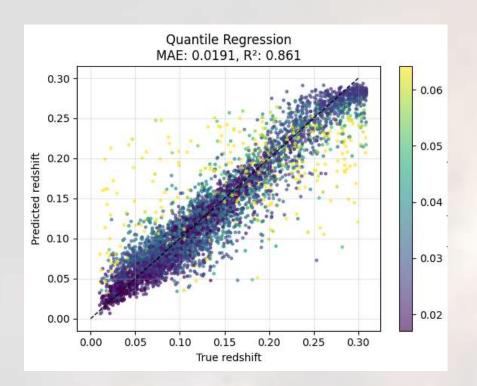




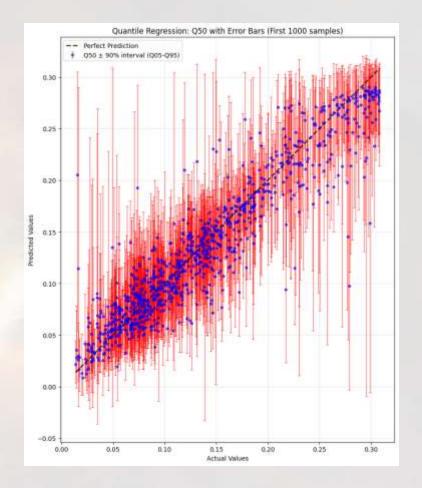




### **Quantile Regression**



90% Coverage: 0.922 IQR [Q<sub>075</sub>(z)-Q<sub>0.25</sub>(z)]: 0.0319







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### **Conformal Prediction**





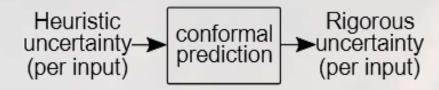


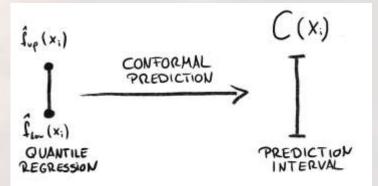


#### **Regression task: age estimation**

Model prediction: 24

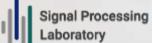
MAPIE prediction interval: [20, 29] (with 90% confidence)

















# **Conformal Prediction**

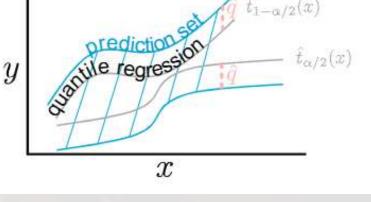
1. Split training data to proper training set and calibration

- 2. Train lower and upper-quantile regressors  $\widehat{Q}^{\alpha/2}, \, \widehat{Q}^{1-\alpha/2}$
- 3. On the calibration set, compute

$$s_i^{\text{CQR}} = \max\left\{y_i^c - \widehat{Q}^{1-\alpha/2}(x_i^c), \ \widehat{Q}^{\alpha/2}(x_i^c) - y_i^c\right\}$$

4. Compute the empirical  $(1 - \alpha)$ -th quantile of the scores:

$$\widehat{q}^{\text{CQR}} = \begin{cases} s^{\text{CQR}}_{\lceil (1-\alpha)(n^c+1) \rceil}, & \text{if } \alpha \geq \frac{1}{n^c+1}, \\ \infty, & \text{otherwise.} \end{cases}$$



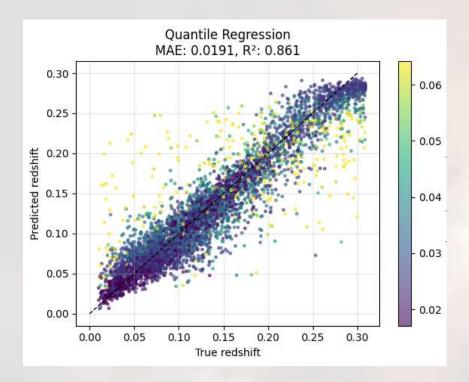
Romano, Y., Patterson, E., & Candes, E. Conformalized quantile regression. *NeurIPS 2029*.

5. Output the coverage interval:

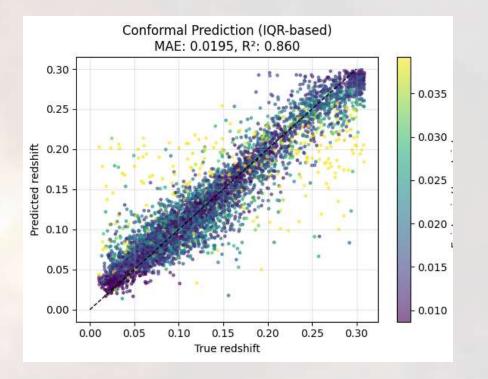
$$\mathcal{C}^{\mathrm{CQR}}(x) = \begin{bmatrix} \widehat{Q}^{\alpha/2}(x) - \widehat{q}^{\mathrm{CQR}}, \ \widehat{Q}^{1-\alpha/2}(x) + \widehat{q}^{\mathrm{CQR}} \end{bmatrix}$$

$$\overset{\text{TITAN}}{\overset{\text{ATTFCAL INTELLKEPICE}}{\overset{\text{FORTH}}{\overset{\text{ITTCAL INTELLKEPICE}}{\overset{\text{RETUCTURE OF COMPUTER SCIENCE}}} \xrightarrow{\mathrm{Formation}} \widehat{\mathbf{F}} \qquad \underbrace{\mathsf{CosmoStat}}{\overset{\text{CosmoStat}}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}}{\overset{\text{CosmoStat}}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}}{\overset{\text{CosmoStat}}{\overset{\text{CosmoStat}}}{\overset{\text{CosmoStat}}{$$

### **Conformal Prediction**



90% Coverage: 0.922 IQR: 0.0319



90% Coverage: 0.900 IQR: 0.0184







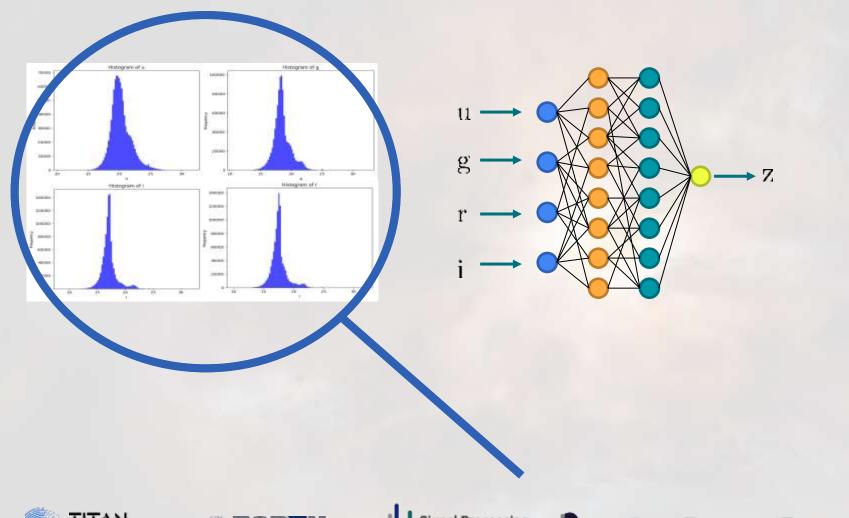
Signal Processing

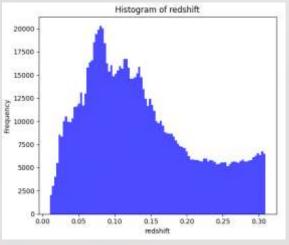






### **Uncertainties (data)**









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### **Ensembles**

- Let  $f^{(m)}(\cdot; \mathbf{w}^{(m)})$  be M independently trained ANN
- During inference, forward-propagate through all netw

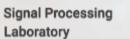
$$\mathbb{E}[y \mid x] \approx \bar{y}(x) = \frac{1}{M} \sum_{m=1}^{M} \hat{y}^{(m)}$$

$$\operatorname{Var}[y \mid x] \approx \frac{1}{M} \sum_{m=1}^{M} (\hat{y}^{(m)})^2 - \bar{y}(x)^2$$









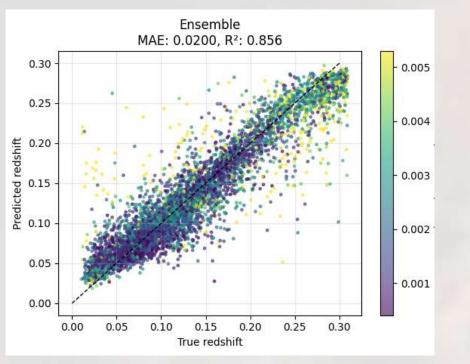


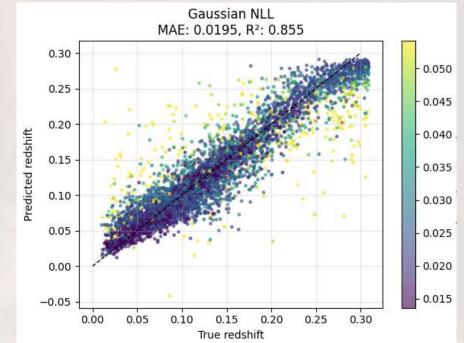




# **Ensemble approach**

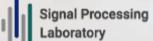
5 Models



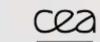














### **MCDropout**

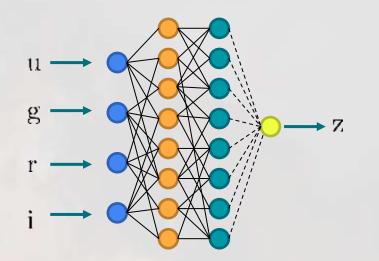
Apply *dropout* to forward pass

$$\hat{y}_i = f(x_i; \mathbf{w} \odot \mathbf{z}_i), \qquad \mathbf{z}_i \sim \text{Bernoulli}(p),$$

### Predictive mean and variance

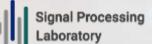
At test time keep dropout on and run S stochastic forward passes  $\hat{y}^{(s)} = f(x; \mathbf{w} \odot \mathbf{z}^{(s)}), s = 1, \ldots, S$ . The predictive posterior moments are approximated by

$$\mathbb{E}[y \mid x] \approx \bar{y} = \frac{1}{S} \sum_{s=1}^{S} \hat{y}^{(s)}, \quad \operatorname{Var}[y \mid x] \approx \frac{1}{S} \sum_{s=1}^{S} (\hat{y}^{(s)})^2 - \bar{y}^2 + \tau^{-1}$$





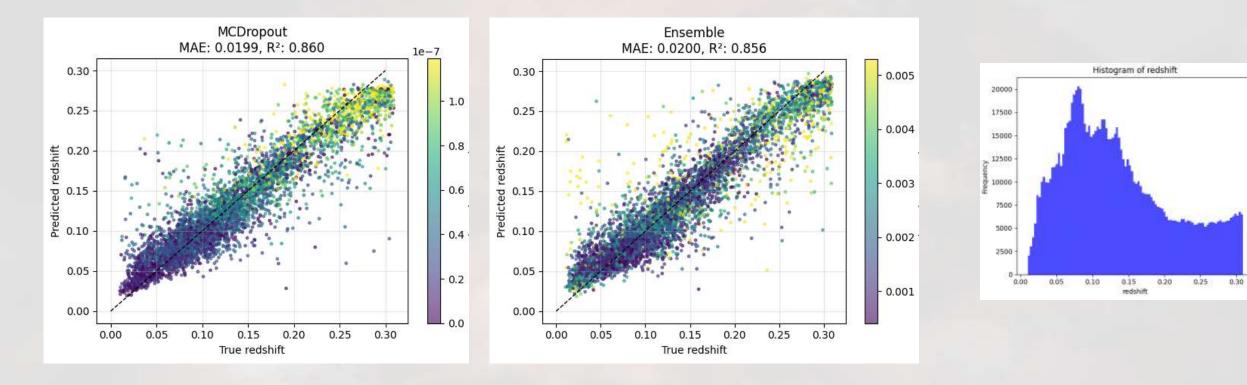








### **MCDropout**









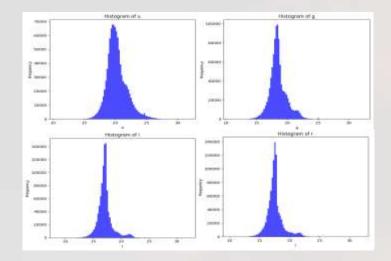
Signal Processing Laboratory

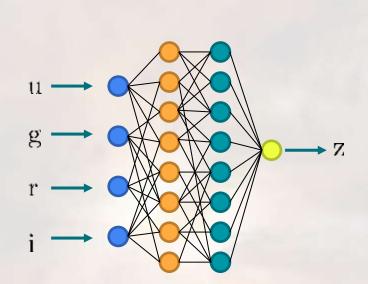


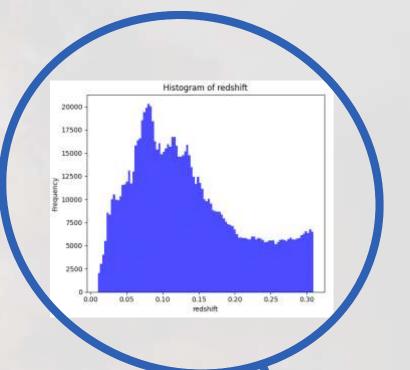




### **Uncertainties (labels)**













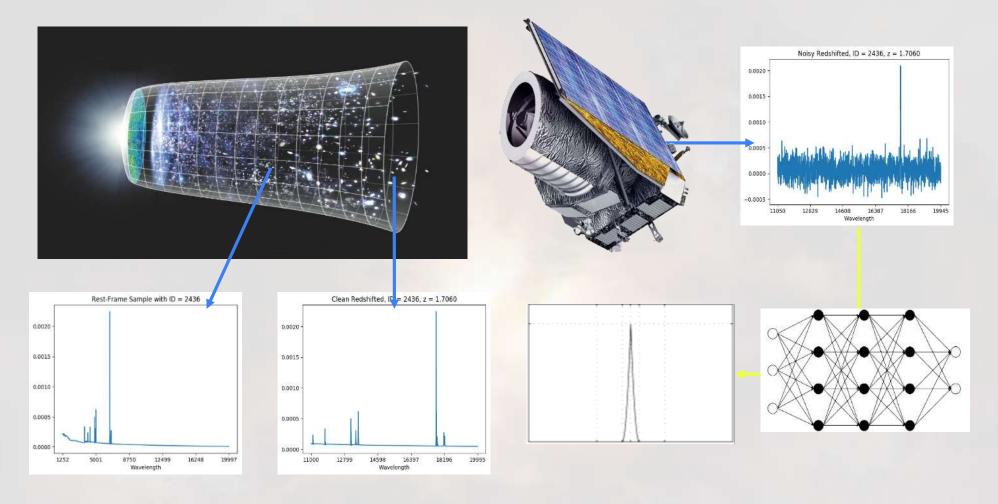






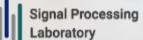


### **Spectroscopic Red-Shift Estimation**















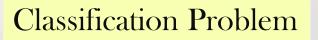
### **Predictive model**

### **Redshift Estimation**



**Regression Analysis** 

Split the examined redshift interval into ordinal classes, based on Euclid's characteristic resolution













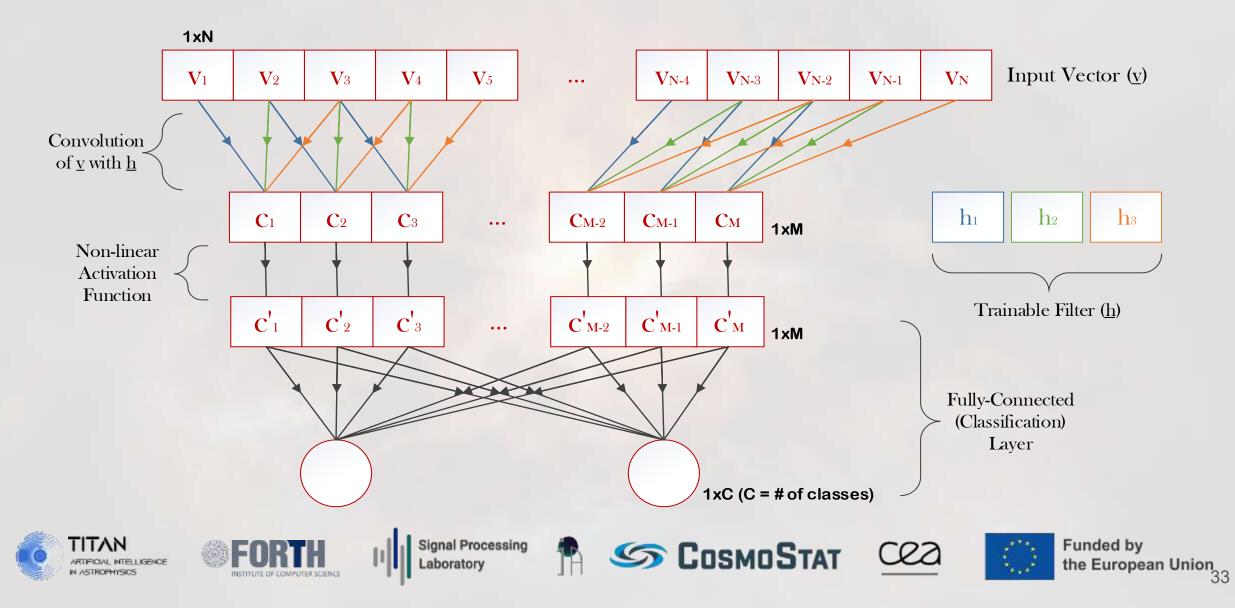






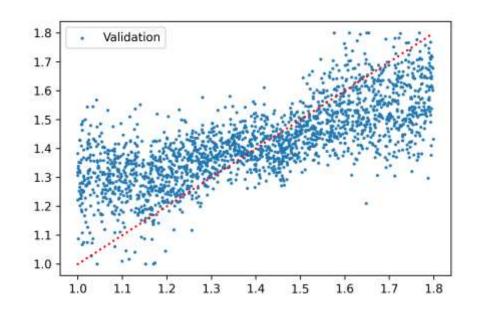


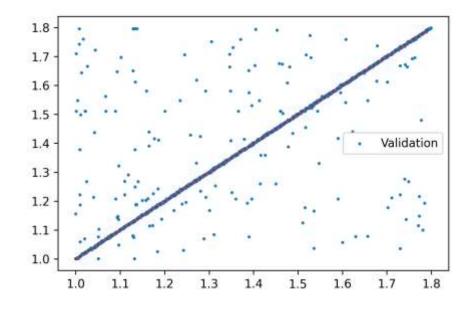
### **1-Dimensional CNN - Classification**



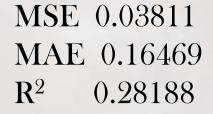


### **Classification (800 classes)**



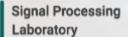


MSE0.00791MAE0.02325R<sup>2</sup>0.85082







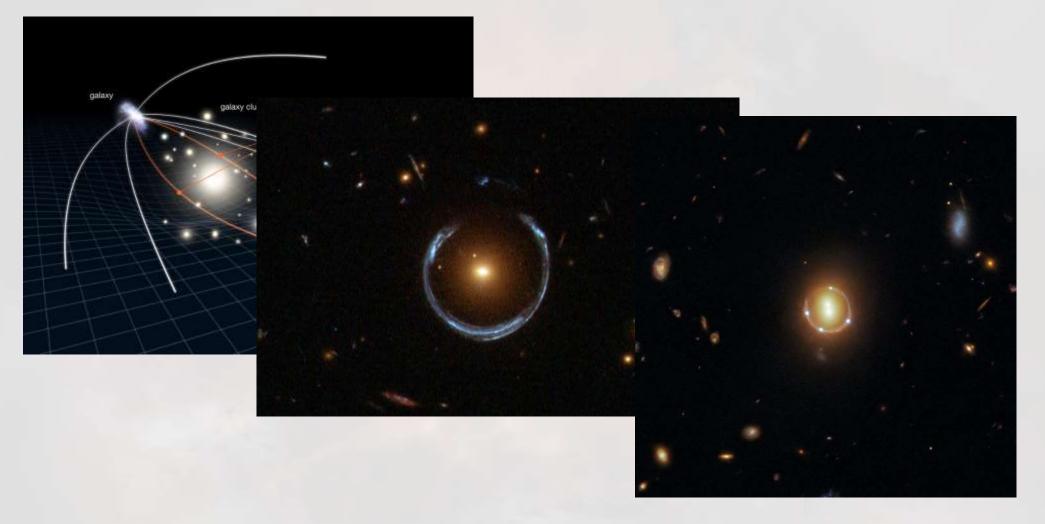




🌀 СоѕмоЅтат



### **Gravitational Lensing**







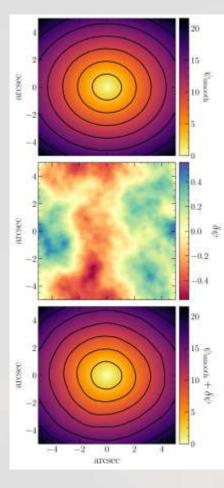








# Modeling with uncertain labels



Singular Isothermal Ellipsoid parametric model

**Realization of Gaussian Random Field** perturbations

#### Perturbed lens potential

G. Vernardos, G. Tsagkatakis, and Y. Pantazis. "Quantifying the structure of strong gravitational lens potentials with uncertainty-aware deep neural networks." MNRAS. 2020.





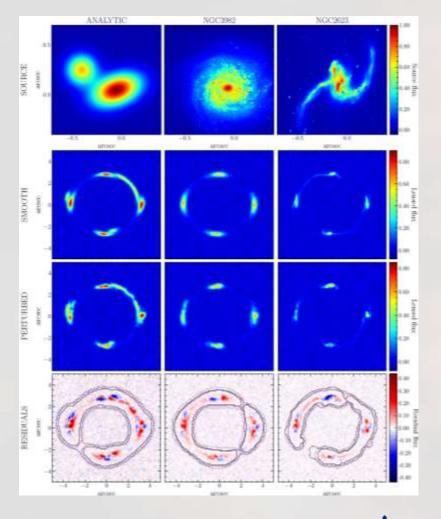
Signal Processing Laboratorv

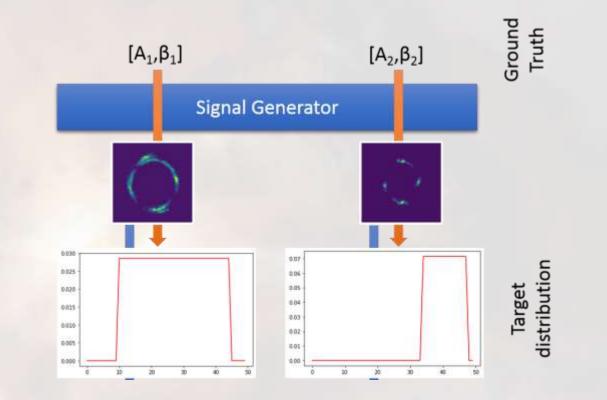






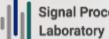
# Label uncertainty

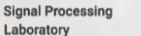








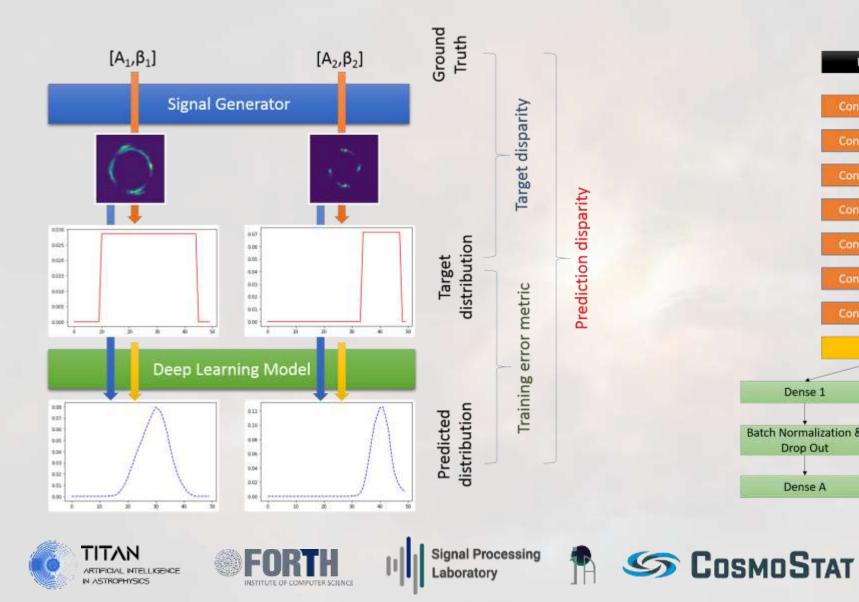








# Modeling with uncertain labels





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# **Modeling with uncertain labels**

Given the predicted distribution P and the target distribution Q, the Jensen-Shannon divergence is defined by:

$$JS(Q, P) = \frac{1}{2}KL(P||M) + \frac{1}{2}KL(Q||M), M = \frac{1}{2}(P+Q)$$

Formally, the entropy of the predicted distribution H(P) is given by:

$$H(P) = -\sum_{x \in \mathcal{X}} P(x) \log(P(x)).$$

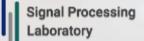
Entropy-regularized version of the JS divergence and is given by:

 $\mathcal{L}(P,Q) = \lambda_1 J S(P,Q) + \lambda_2 H(P),$ 

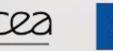
where  $\lambda_1$  and  $\lambda_2$  control the impact of the two terms.



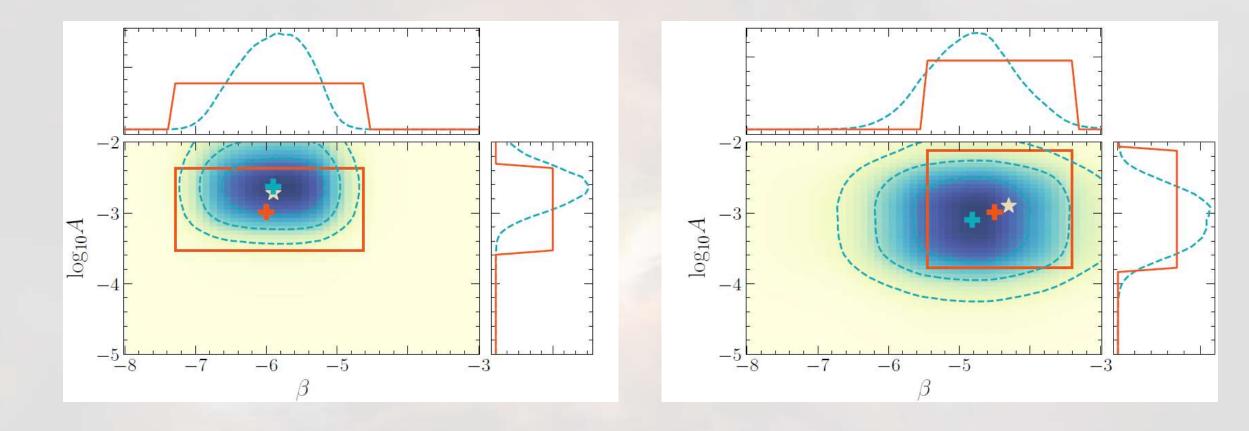






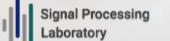


# "Label-super-resolution"













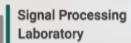


# **Take-home messages**

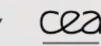
- Many flavors of uncertainty (decoupling, Bayesian, ordinal regression)
- "Limited" investigation in scientific data analysis
- The case of time-domain astronomy
- The case of spatially resolved observations
- The promise of multi-modality

















MINOAS - Machine Intelligence for iNverse imaging,
Observation Analysis and Sensing Workshop
Dates: 24-26 September 2025
Location: FORTH, Crete





